

Attack–Defense Tree Methodology for Security Assessment

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- 1 Attack–defense trees
- 2 Semantics
- 3 Quantitative analysis
- 4 Computational complexity
- 5 Attack–defense trees in practice

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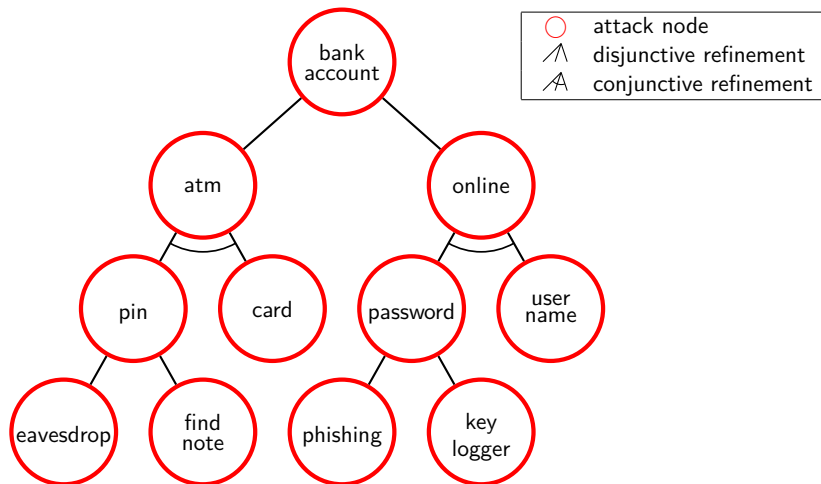
Definition

Attack tree (ATree) – tree-like representation of an attacker's goal recursively refined into conjunctive or disjunctive sub-goals.

Methodology to describe security weaknesses of a system

- Proposed by Schneier
Attack trees: Modeling Security Threats, '99
- Formalized by Mauw and Oostdijk
Foundations of Attack Trees [ICISC'05]

Example: attacking a bank account



Limitations of attack trees

- Only attacker's point of view
- No defensive measures
- No attacker/defender interactions
- No evolutionary aspects

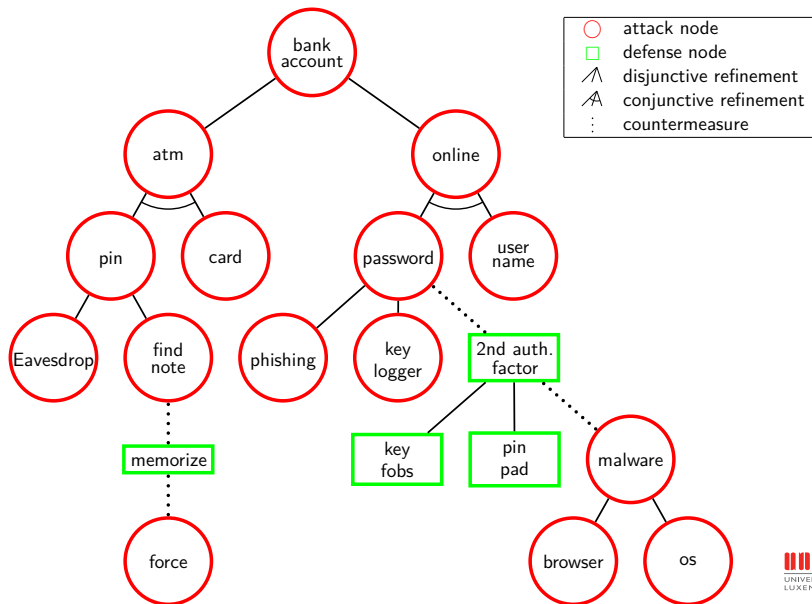
Definition

Attack–defense tree (ADTree) – attack tree extended with possibly refined or countered defensive actions.

Introduced by Kordy et al. in

Foundations of Attack–Defense Trees [FAST'10]

Example: attacking and defending a bank account



Interesting questions

- Equivalent representations of the same scenario (semantics)
- Quantitative analysis (attributes)
- Computational complexity of ATrees and ADTrees (querying)
- Practical applications (case studies)

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Semantics define which ADTrees represent the same scenario.

Definition

Semantics for ADTrees – equivalence relation on ADTrees.

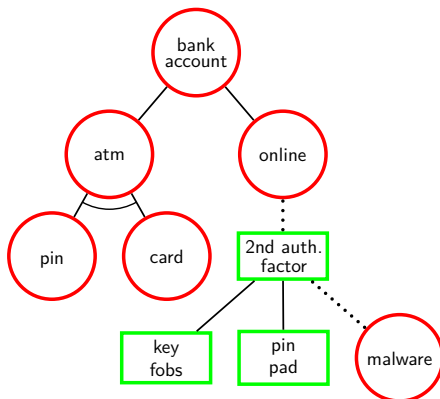
- Propositional semantics
- Semantics induced by a De Morgan lattice
- Multiset semantics
- Equational semantics

In the propositional semantics

ADTrees represent Boolean functions.

Example: propositional interpretation of an ADTree

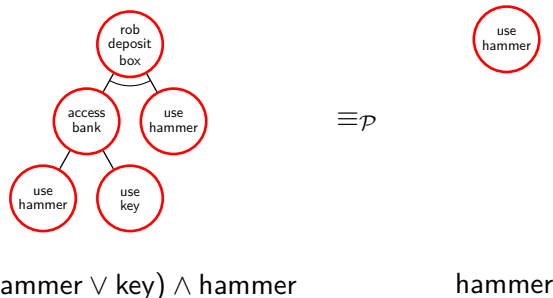
$$f = (\text{pin} \wedge \text{card}) \vee (\text{online} \wedge \neg((\text{key fobs} \vee \text{pin pad}) \wedge \neg \text{malware}))$$



In the propositional semantics

ADTress represent the same scenario if the corresponding Boolean functions are equivalent.

Example: propositionally equivalent ADTrees



The two trees are equivalent in the propositional semantics, because in propositional logics we have absorption law

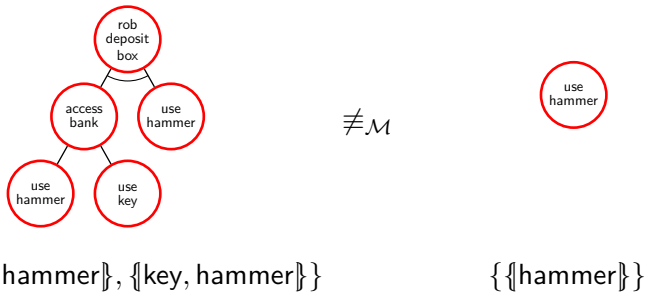
$$(\text{hammer} \vee \text{key}) \wedge \text{hammer} \equiv \text{hammer}$$

ADTrees are interpreted as sets of multisets.
Each multiset represents a possible way of attacking.

In the multiset semantics

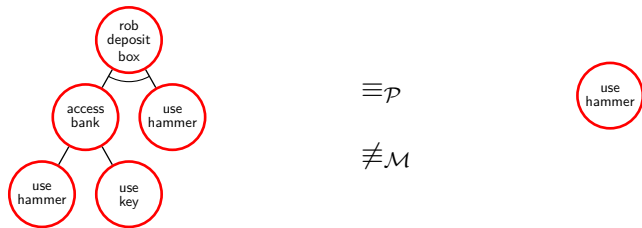
ADTrees represent the same scenario if the corresponding sets of multisets are equal.

Example: ADTrees not equivalent in the multiset semantics



The two trees are not equivalent in the multiset semantics, because $\{\{\text{hammer, hammer}\}, \{\text{key, hammer}\}\} \neq \{\{\text{hammer}\}\}$.

Different semantics – different equivalence classes



The choice of an appropriate semantics

depends on considered applications and assumptions.

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Quantitative analysis of an attack–defense scenario

- Standard questions
 - What is the minimal cost of an attack?
 - What is the expected impact of a considered attack?
 - Is special equipment required to attack?
- Bivariate questions
 - How long does it take to secure a system, when the attacker has a limited budget?
 - How does the scenario change if both, the attacker and the defender are affected by a power outage?

Bottom-up algorithm

- Basic assignment – values assigned to basic actions
 - Attribute domain – operators specifying how to compute values for other nodes
-
- Intuitive idea of Schneier
Attack trees: Modelling Security Threats, '99
 - Formalization by Mauw and Oostdijk for attack trees
Foundations of Attack Trees, [ICISC'05]
 - Extension to attack–defense trees by Kordy et al.
Foundations of Attack–Defense Trees, [FAST'10]

Attribute: minimal time of an attack

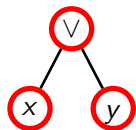
Question:

What is the minimal time needed to achieve a considered attack?

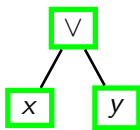
Attribute domain:

- Values from $\mathbb{N} \cup \{\infty\}$
- ∞ = action not under control of the attacker
- $(\vee^A, \wedge^A, \vee^D, \wedge^D, c^A, c^D) = (\min, +, +, \min, +, \min)$

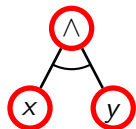
Attribute domain for *minimal time*



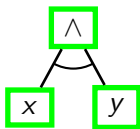
$$\vee^A: \min\{x, y\}$$



$$\vee^D: x + y$$



$$\wedge^A: x + y$$



$$\wedge^D: \min\{x, y\}$$



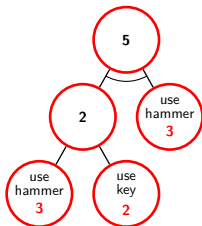
$$c^A: x + y$$



$$c^D: \min\{x, y\}$$

Example: computation of *minimal time* on an ADTree

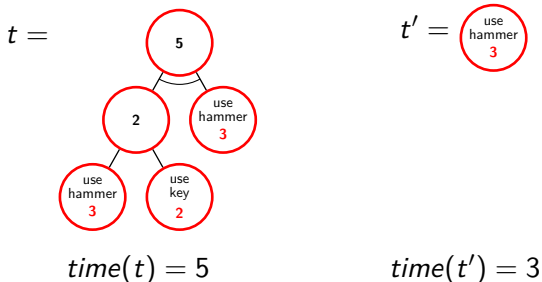
$$(\vee^A, \wedge^A, \vee^D, \wedge^D, c^A, c^D) = (\min, +, +, \min, +, \min)$$



► Details

Semantics and attribute domains

Recall: t and t' are equivalent in the propositional semantics.



- Problem: $t \equiv_{\mathcal{P}} t'$, but $time(t) \neq time(t')$
- Solution: Compatibility notion

Compatibility of an attribute with a semantics

Compatibility defines which semantics should be used in combination with which attribute.

Definition

Attribute α is compatible with semantics \equiv for ADTrees iff $\forall t, t' \in \text{ADTrees}, t \equiv t' \implies \alpha(t) = \alpha(t')$.

- Problem: How to check compatibility?
- Solution: Complete set of axioms for a semantics.

► Details

Definition

A set E of ADTree transformations is a **complete set of axioms for a semantics** for ADTrees iff equivalent ADTrees can be obtained from each other by application of transformations from E .

- Problem: How to find a complete set of axioms for a semantics?
- Solution: This is difficult. . .

Complete set of axioms

We have identified complete sets of axioms for

- the propositional semantics (44 transformations)
 - using minimal DNF representation of propositional formulas
- the multiset semantics (22 transformations)
 - using term rewriting techniques

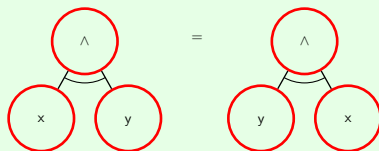
Details can be found in [Attack-Defense Trees \(to appear in JLC'12\)](#).

Axiomatization and compatibility

Using a complete set of axioms, compatibility can be decided by performing a finite number of easy checks.

Example

- Transformation – commutativity of attacker's AND refinement



- Corresponding equation for *minimal time* attribute

$$x + y = y + x \text{ holds in } \mathbb{N}.$$

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- ADTrees enrich modeling capabilities of ATrees.
- How much computational power do they require w.r.t. ATrees?

Boolean functions represented by ATrees and ADTrees

In *Computational Aspects of Attack–Defense Trees* [SIIS'11], we show

Lemma

- 1 *ATrees represent positive Boolean functions.*
- 2 *ADTrees represent monotone Boolean functions.*

Theorem

Every monotone Boolean function, which is not positive, can be brought into a positive form in linear time.

Corollary (Kordy, Pouly, Schweitzer [SIIS'11])

When the propositional semantics is used, the computational complexity of ADTrees is the same as the computational complexity of ATrees.

When the propositional semantics is used

- ADTrees can be processed by algorithms developed for ATrees.
- Complexity of query evaluation on ADTrees is the same as the corresponding complexity on ATrees.
- Queries that can efficiently be solved on ATrees can also efficiently be solved on ADTrees.

Limitations of the propositional semantics

b

$$f(b) = b$$

b

$$f(b) = b$$

- The Boolean function $f: \{0, 1\}^b \rightarrow \{0, 1\}$ corresponding to a non-refined node b is of the form $f(b = v) = v$, where $v \in \{1, 0\}$.
- This means that the propositional semantics assumes that each component which is present is fully effective.
- Problem: Such strong assumption is not always desirable.

Example: modeling effectiveness level of an attack

Let $\{F, M, T\}$ be a set of effectiveness levels, where $F < M < T$.



- Boolean function given by $f(d = 1) = 1$ and $f(d = 0) = 0$ is not well suited to model effectiveness level of a dictionary attack.
- We need a function of the form $f: \{0, 1\}^{\{d\}} \rightarrow \{F, M, T\}$, where $f(d = 1) = M$ and $f(d = 0) = F$.

In semantics induced by a De Morgan lattice L

ADTrees represent functions of the form $f: \{0, 1\}^X \rightarrow L$, where X is a set of propositional variables.

- De Morgan lattices allow us to use more than only two values 0 and 1.
- Semantics induced by De Morgan lattices allow for more accurate analysis, with respect to the propositional semantics.

► Details

Theorem

When a semantics induced by a De Morgan lattice is used, the computational complexity of ADTrees is the same as the computational complexity of ATrees.

When ADTrees represent functions of the form

- $f: \{0, 1\}^X \rightarrow \{0, 1\}$
- $f: \{0, 1\}^X \rightarrow L$, with L a De Morgan lattice

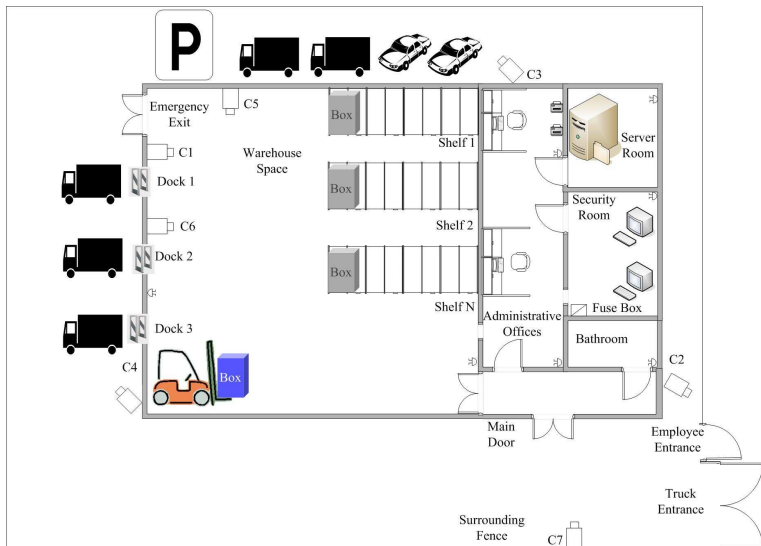
enriching the attack tree formalism with defense nodes is not done at the expense of computational complexity.

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- Objectives: checking usefulness of the ADTree methodology
 - test
 - validate
 - define tool requirements
 - improve the formalism
- Partners:
 - SINTEF, Norway (Per Håkon Meland)
 - TXT e-solutions, Italy (Alessandra Bagnato)
- Results: *Attribute Decoration of Attack–Defense Trees* [IJSSE'12]

Case study scenario

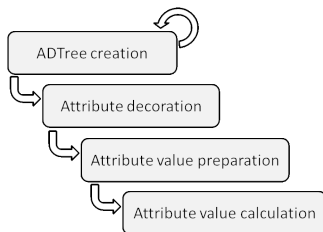
DoS in RFID-based goods management system



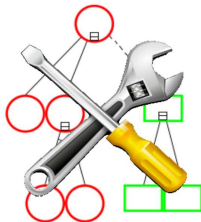
- ADTree of 97 nodes
- Taking into account multiple aspects:
 - physical access,
 - social engineering attacks,
 - digital attacks.
- Evaluation of 10 attributes: *cost, time, detectability, penalty, skill level, impact, difficulty, profitability*

Case study outcomes

- Guidelines explaining how to use ADTrees in practice



- Requirements for an ADTree software



ADTool

Software tool supporting the ADTree methodology.

- Implemented in Java.
- Compatible with multiple platforms.
- Graphical user interface.
- Supports attribute evaluation on ADTrees.

Main features of ADTool

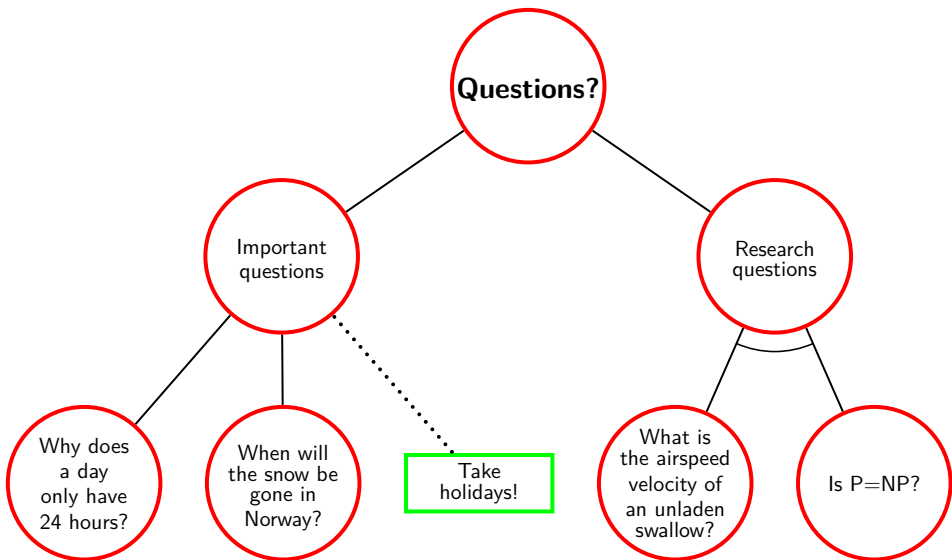
- Creation of ADTrees.
- Modular display of ADTrees – necessary in case of large trees.
- Evaluation of predefined attributes, including:
 - *minimal cost of an attack,*
 - *minimal skill of the winner,*
 - *satisfiability of an attack,*
 - *cheapest satisfiable attack,*
 - *minimal attack time,*
 - *attack satisfiable in less than 10 minutes.*
- Possibility of defining new attributes.

Summary

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- Research questions
 - Probabilistic analysis: ADTrees & Bayesian networks
 - Access control analysis: ADTrees & policy trees
- Further testing and development of ADTool
 - Release planned for summer 2012
- Future projects: ADTrees for socio-technical security
 - EU: TREsPASS
 - CORE-FNR: STAST

Thank you for your attention!



References

-  [FAST'10] Kordy, Mauw, Radomirović and Schweitzer
Foundations of Attack–Defense Trees. In Proceedings of FAST 2010, volume 6561 of LNCS. Springer 2011.
-  [GameSec'10] Kordy, Mauw, Melissen and Schweitzer
Attack-defense trees and two-player binary zero-sum extensive form games are equivalent. In Proceedings of GameSec 2010, volume 6442 of LNCS. Springer, 2010.
-  [SIIS'11] Kordy, Pouly and Schweitzer
Computational Aspects of Attack–Defense Trees. In Proceedings of SIIS 2011, volume 7053 of LNCS. Springer, 2011.
-  [JLC'12] Kordy, Mauw, Radomirović and Schweitzer
Attack–Defense Trees. To appear in Journal of Logic and Computation.
-  [IJSSE'12] Bagnato, Kordy, Meland and Schweitzer
Attribute Decoration of Attack–Defense Trees. To appear International Journal of Secure Software Engineering, Special Issue on Security Modeling.

APPENDIX

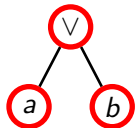
ADTrees as Boolean functions



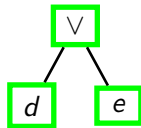
$$f(a) = a$$



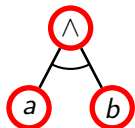
$$f(d) = d$$



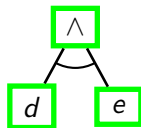
$$f(a, b) = a \vee b$$



$$f(d, e) = d \vee e$$



$$f(a, b) = a \wedge b$$



$$f(d, e) = d \wedge e$$



$$f(a, d) = a \wedge \neg d$$

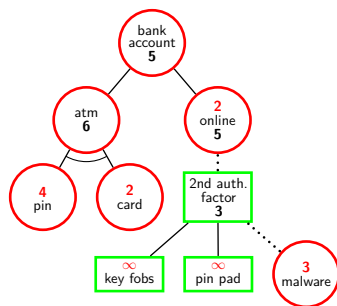


$$f(d, a) = d \wedge \neg a$$

▶ Back

Example: computation of *minimal time* on an ADTree

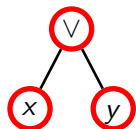
$$(\vee^A, \wedge^A, \vee^D, \wedge^D, c^A, c^D) = (\min, +, +, \min, +, \min)$$



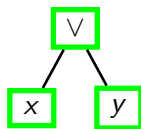
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α -expressions for ADTrees

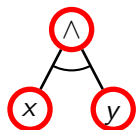
Given an attribute domain $\alpha = (\mathbb{D}, \vee^A, \wedge^A, \vee^D, \wedge^D, c^A, c^D)$ we set



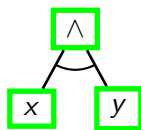
$$t_\alpha = \vee^A(x, y)$$



$$t_\alpha = \vee^D(x, y)$$



$$t_\alpha = \wedge^A(x, y)$$



$$t_\alpha = \wedge^D(x, y)$$



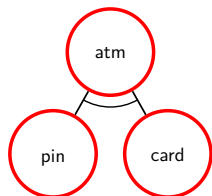
$$t_\alpha = c^A(x, y)$$



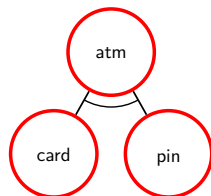
$$t_\alpha = c^D(x, y)$$

Example: *minimal_time*-expressions for ADTrees

$$time = (\mathbb{N} \cup \{\infty\}, \min, +, +, \min, +, \min)$$



$$t_{time} = \text{pin} + \text{card}$$



$$t'_{time} = \text{card} + \text{pin}$$

$$t_{time} = t'_{time} \text{ in } \mathbb{N} \cup \{\infty\}$$

because $+$ is commutative on $\mathbb{N} \cup \{\infty\}$

Definition

Attribute domain $\alpha = (\mathbb{D}, \vee^A, \wedge^A, \vee^D, \wedge^D, c^A, c^D)$ is **compatible with semantics** \equiv if and only if

$$\forall t, t' \in ADTrees, \quad t \equiv t' \Rightarrow t_\alpha = t'_\alpha \text{ holds in } \mathbb{D}.$$

Theorem

If an attribute domain is compatible with a semantics, then equivalent ADTrees yield the same attribute values.

Example: incompatibility of *minimal time* with $\equiv_{\mathcal{P}}$

$$time = (\mathbb{N} \cup \{\infty\}, \min, +, +, \min, +, \min)$$

time is not compatible with the propositional semantics $\equiv_{\mathcal{P}}$

- $(a \vee^{\mathcal{P}} b) \wedge^{\mathcal{P}} a \equiv_{\mathcal{P}} a$, since $(a \vee b) \wedge a \approx a$
- but $(a \min b) + a \neq a$ in $\mathbb{N} \cup \{\infty\}$.

Definition

Attribute domain $\alpha = (\mathbb{D}, \vee^A, \wedge^A, \vee^D, \wedge^D, c^A, c^D)$ is **compatible with semantics** \equiv if and only if

$$\forall t, t' \in ADTrees, \quad t \equiv t' \Rightarrow t_\alpha = t'_\alpha \text{ holds in } \mathbb{D}.$$

- Problem: How to find all t, t' , such that $t \equiv t'$?
- Solution: Axiomatization of semantics

▶ Back

De Morgan lattice

- L – non-empty set
- $+$, \times – binary operations on L
- \neg – unary operation on L

Definition

$\langle L, +, \times, \neg \rangle$ is a **De Morgan lattice** if $\langle L, +, \times \rangle$ is a distributive lattice and, for all $a, b \in L$, we have

$$\neg(a + b) = (\neg a) \times (\neg b), \quad \neg(a \times b) = (\neg a) + (\neg b), \quad \neg(\neg a) = a.$$

Example

De Morgan lattice $\langle \{F, M, T\}, \max, \min, \neg \rangle$, with

- $F < M < T$,
- $\neg F = T$, $\neg M = M$, $\neg T = F$,

may represent effectiveness levels.

Semantics induced by a De Morgan lattice

X = finite set of propositional variables

$\langle L, +, \times, \neg \rangle$ = De Morgan lattice

Definition

A **De Morgan valuation** (DMV) with domain d is a function of the form $f: \{0, 1\}^X \rightarrow L$.

ADTrees form a representation language for De Morgan valuations:

$$\begin{aligned} f_b(X_b = v) &= l_v & f_{\vee^s}(t_1, \dots, t_k) &= \sum_{i=1}^k f_{t_i}, \\ f_{\wedge^s}(t_1, \dots, t_k) &= \prod_{i=1}^k f_{t_i}, & f_{\text{C}^s}(t_1, t_2) &= f_{t_1} \times \neg f_{t_2}, \end{aligned}$$

where $v \in \{1, 0\}$, $l_v \in L$ and $s \in \{A, D\}$. [▶ Back](#)