



### A Game-Theoretic Framework for Analyzing Trust-Inference Protocols

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## Introduction

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- - $\Pi_1$  Proof

### Why is trust necessary in P2P?

- Cooperation is necessary
- Simple punish/incentive scheme using own interactions is problematic (rare direct interaction = low chance of redeem, the first time problem...)
- Use the other agents' interactions (propagated in the system) → reputation/recommendation system

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### The provided definition

- Enables proofs
- Enables comparisons
- Is appropriate for decentralized systems
- Enables the use of a wide range of adversarial behavior

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- Pseudonyms are
- Distinct (unique)
- Easy to create by the users themself (no trusted party)
- Impossible to impersonate by others
- Protocol  $\Pi$  prescribes
- how trust should be infered
- how a user's actions should depend upon the inferred value

## The Adversarial Framework

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Adversary *A*'s oracles (=actions)

- NewUser creates a new honest user and A learns it
- HonestPlay(i,j) 2-players game according to the protocol Π between *i* and *j*
- Play(i, id, action) 2-players game between A (id) and i (honest player)
- $\blacksquare$  Send(i, id, msg) A sends a message msg to i
- $\blacksquare$  + A can see any message between honest users

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Rational adversaries are assumed

Adversary's utility increases after each *Play* by  $\delta^t \mu$  where  $\mu$  is the payoff (cf. table) and  $\delta < 1$  is a discount factor

## Network model

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### Broadcast Network reliable

### Complete P2P Network trusted infrastructure (?)

- Every user learns the arrival of a new user
- Any user can send messages to others using the infrastructure
- NotifyJoin(i,j) additional A's oracle

### Timing Model - part1/2

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- In a time period t
- A makes at most N NewUser calls
- A makes at most N' Play calls

The value t always increases and each time period is divided into play phase and protocol phase

- play phase: A can issue NewUser, Play, and HonestPlay
- play phase ends at first Send Or Activate call (stamped with t)
- protocol phase: Send, Activate, Done, and messages between honest users are exchanged
- protocol phase ends when A makes a call stamped with t + 1

## Timing Model - part2/2

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- But A can label a call with t + 1 only if
- in protocol phase of t
- the last n calls where Activate answered with Done (n is the number of current honest users)

In addition, A cannot issue a *Play* on a honest user created in the current period

## Robustness

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**Definition 1**: " $\Pi$  is robust if A maximizes its utility by following  $\Pi$ , i.e. if the actions prescribed by  $\Pi$  form a subgame-perfect equilibrium"

### Other notions:

- **Expected utility**: utility when everyone is honest
- Resilience to trembles: "honest" defects (network fault ...)
- Efficiency at admitting newcomers: not too severe penalty
- Efficiency: number of messages ...

## $\Pi_1 - \mathbf{Grim} \ \mathbf{Trigger}$

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- A player that has never received a grim trigger message always cooperate
- If players i and j interact and i defects, then j sends a grim trigger message to everyone (and himself) in the following protocol phase
- A player that has received a grim trigger message will always defect and will send grim trigger messages to everyone at every subsequent time period

**Lemma 1**: "The grim trigger strategy is robust if the future (?) discount factor  $\delta$  is at least  $\frac{1}{2}$ , and it achieves optimal expected utility when the probability of trembles is 0, in the strongest adversarial model considered here"

# $\Pi_1 - \mathbf{Proof}$

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■ Let adversary *G* be compliant with the protocol (no defect)

- G creates N honest users at  $t_0$
- t > 0, G fair-Plays with each honest user

• The utility of *G* is : 
$$u_G = \sum_{t=1}^{\infty} N\delta^t = \frac{N\delta}{1-\delta}$$

• If A defects at time t', its utility is:

$$u_A = \sum_{t=1}^{t'-1} N\delta^t + 2N\delta^{t'} = \frac{N\delta(1-\delta^{t'})}{1-\delta} + N\delta^{t'}$$

• Then  $u_A > u_G$  iff  $\delta < \frac{1}{2}$