

# Beyond attack trees: Attack and defense modeling with BDMP (Boolean logic Driven Markov Processes)

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CHANGER L'ÉNERGIE ENSEMBLE

# Agenda

## ▶ Introduction

- Graphical attack modeling and relevance of BDMP

## ▶ Attack and defense modeling with BDMP

- Formalism description
- Theoretical basis and description
- Examples & quantifications

## ▶ Recent advances

- Enhancements and complementary tools

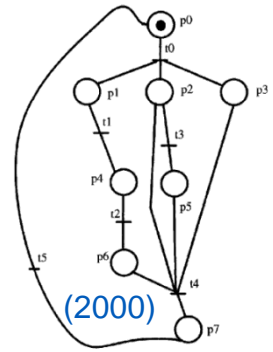
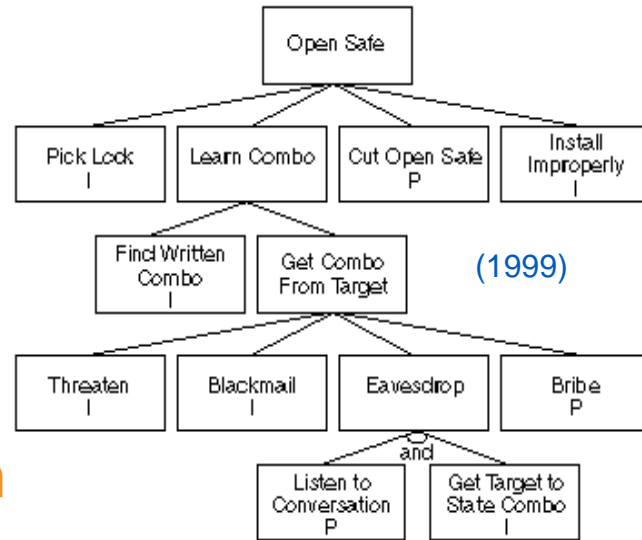
## ▶ Perspectives and on-going work

## ▶ Conclusion and Q&A

# Graphical modeling of computer attacks

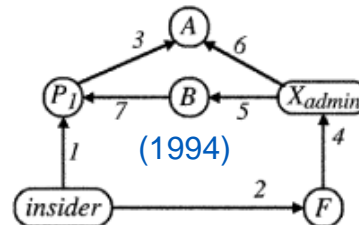
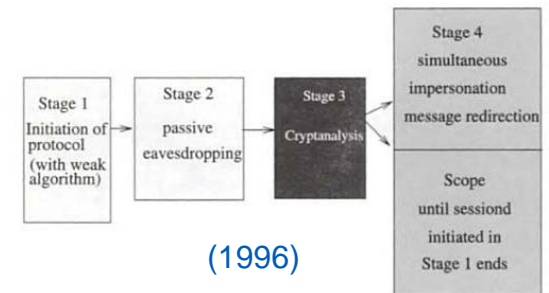
## Graphical representation of an attack process

- Red-team, risk analysis
- Formalize reasoning
- Share standpoints
- Enhance coverage



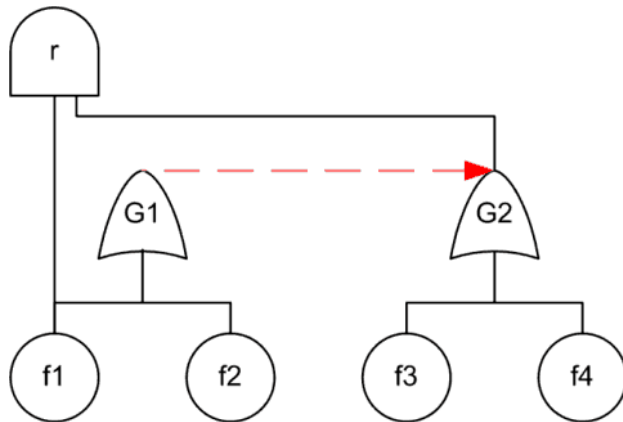
## An active field of research

- Different trade-offs
  - Ease of appropriation
  - Readability
  - Modeling power
  - Quantification capabilities
  - Scalability



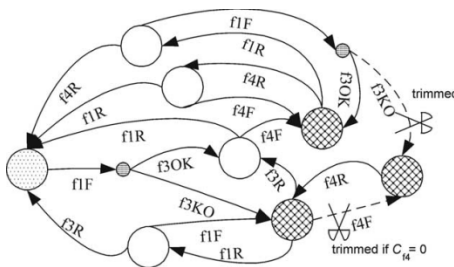
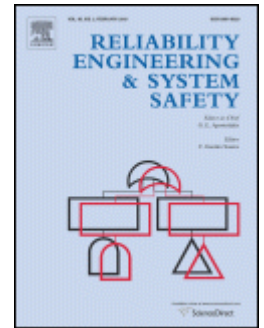
# BDMP, the potential for an attractive trade-off

## ▶ Interest proven in reliability and safety engineering



- ✓ Dynamic
- ✓ Readable
- ✓ Tractable

A new formalism that combines advantages of fault-trees and Markov models: Boolean logic Driven Markov Processes  
*Reliability Engineering and System Safety*, Vol. 82, Issue 2, Nov. 2003, pp.149-163



- Invented and used at EDF (NPP safety, substations, data centers reliability,...)
- Complete theory and software framework

⇒ Adaptation to attack modeling

# BDMP – Application to attack modeling

## ► In a nutshell...

- The look of a classical attack tree

- Objective = *top event*
- Logical gates AND, OR, etc.

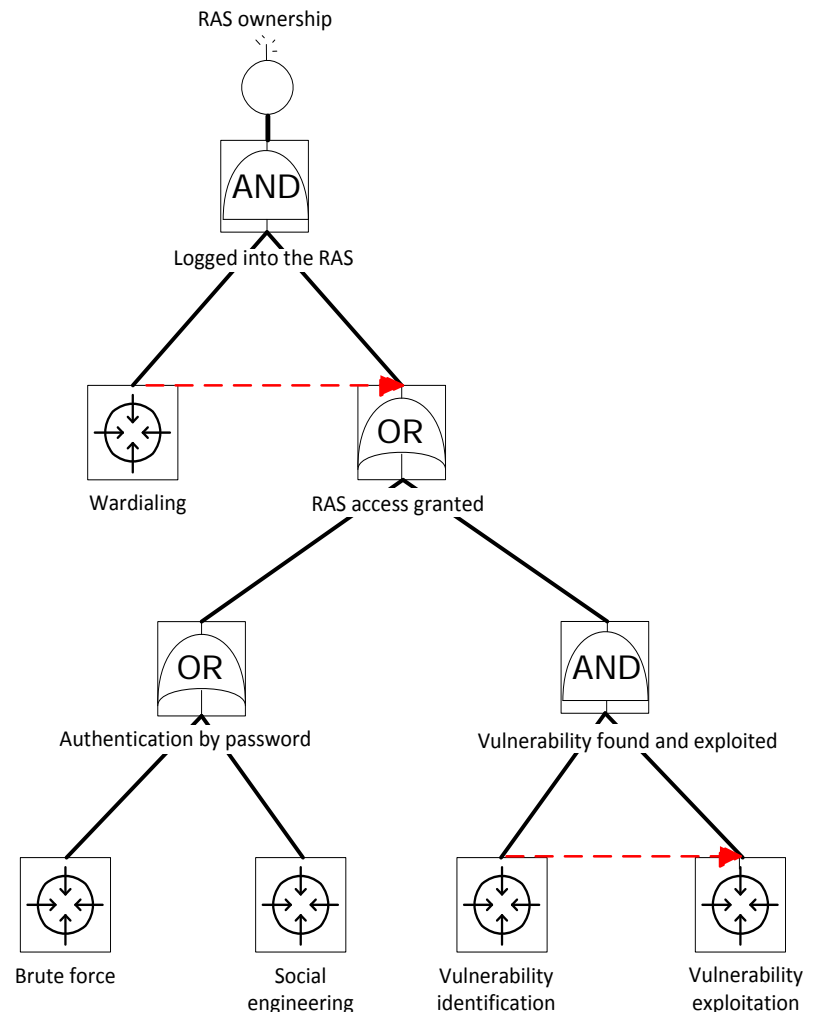
- Triggers  $\{T\}$

- Leaves under two modes

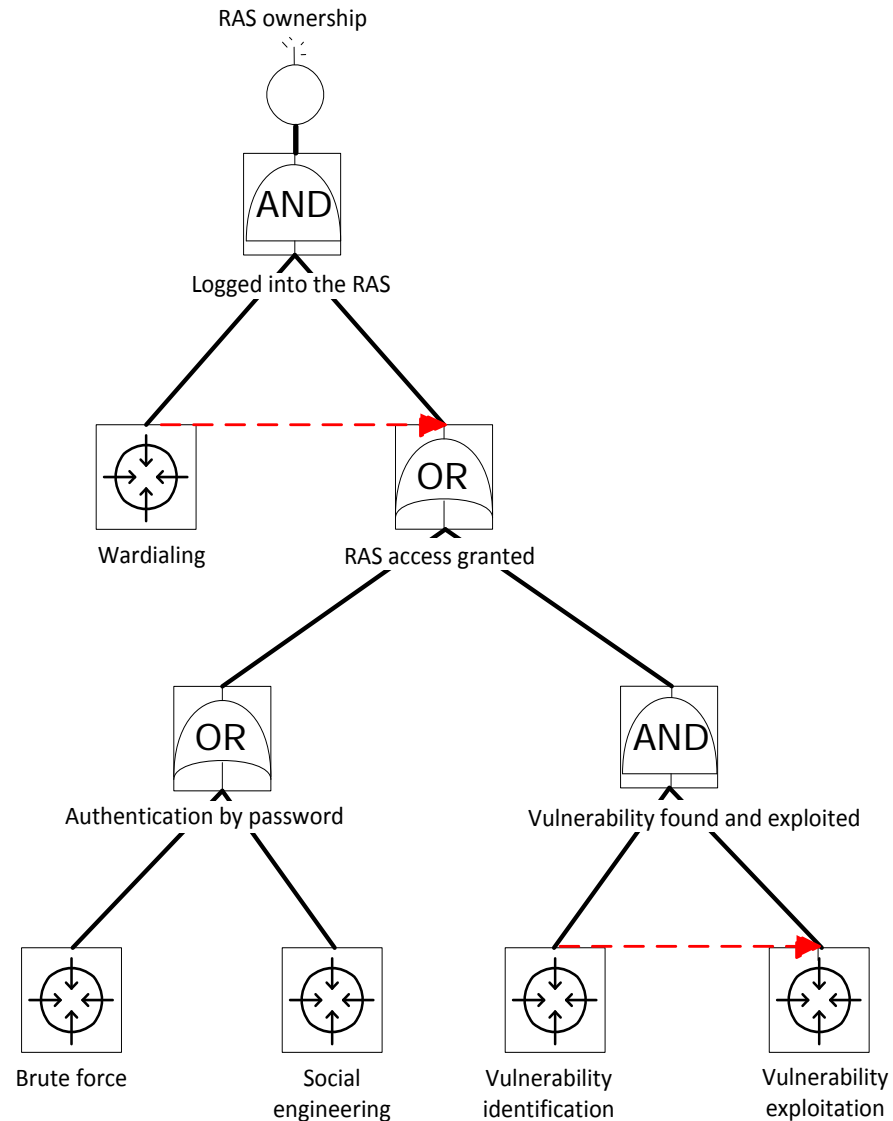
- « Idle » and « Active »
- Triggered Markov processes

## ► Interest of BDMP in security

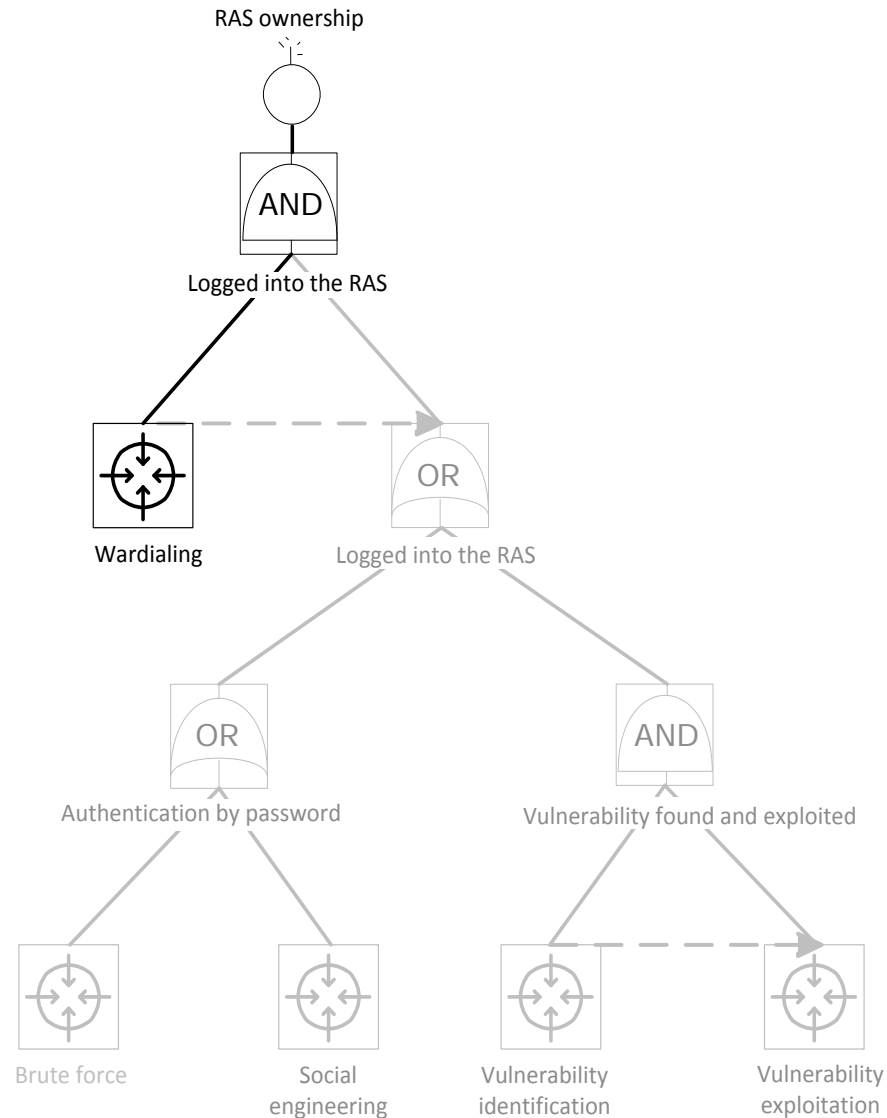
- Dynamical (> attack trees)
- Readable (close to attack trees)



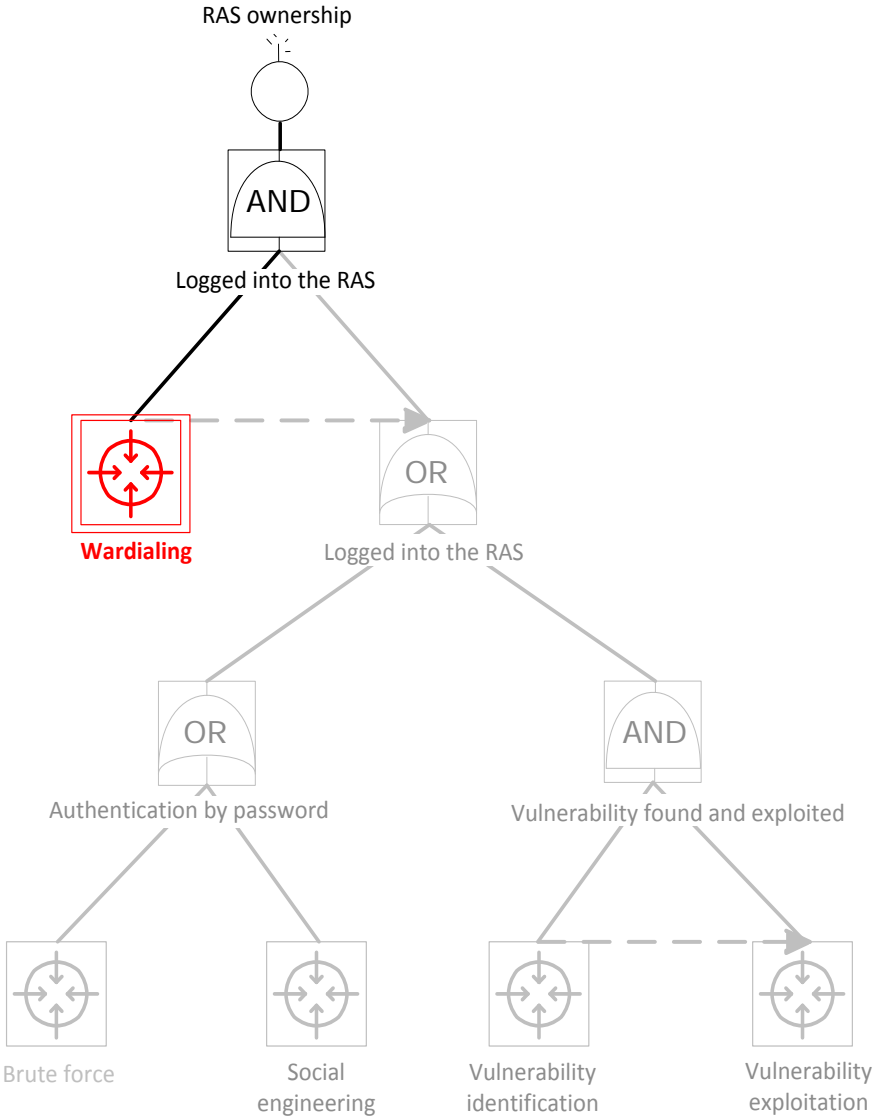
# RAS attack BDMP – A simple use-case



# RAS attack BDMP – Step 0 (attack just started)

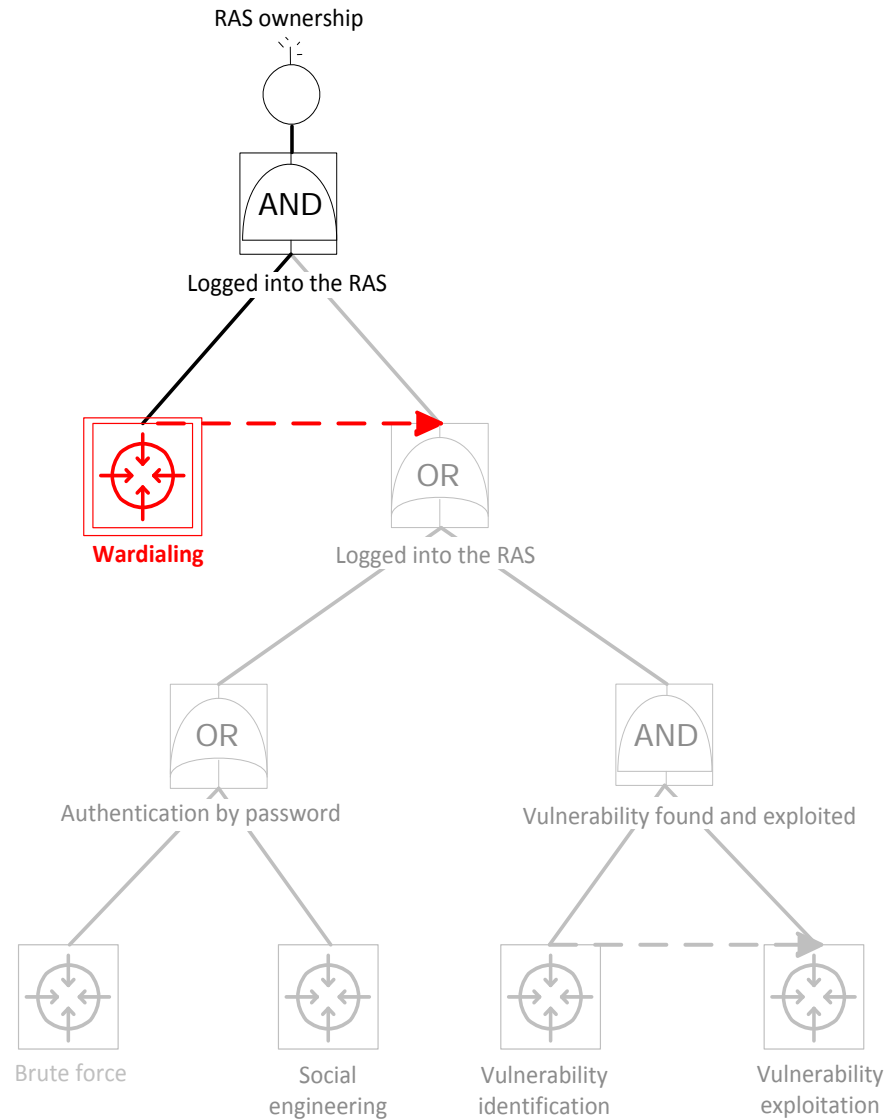


# RAS attack BDMP – Step 1

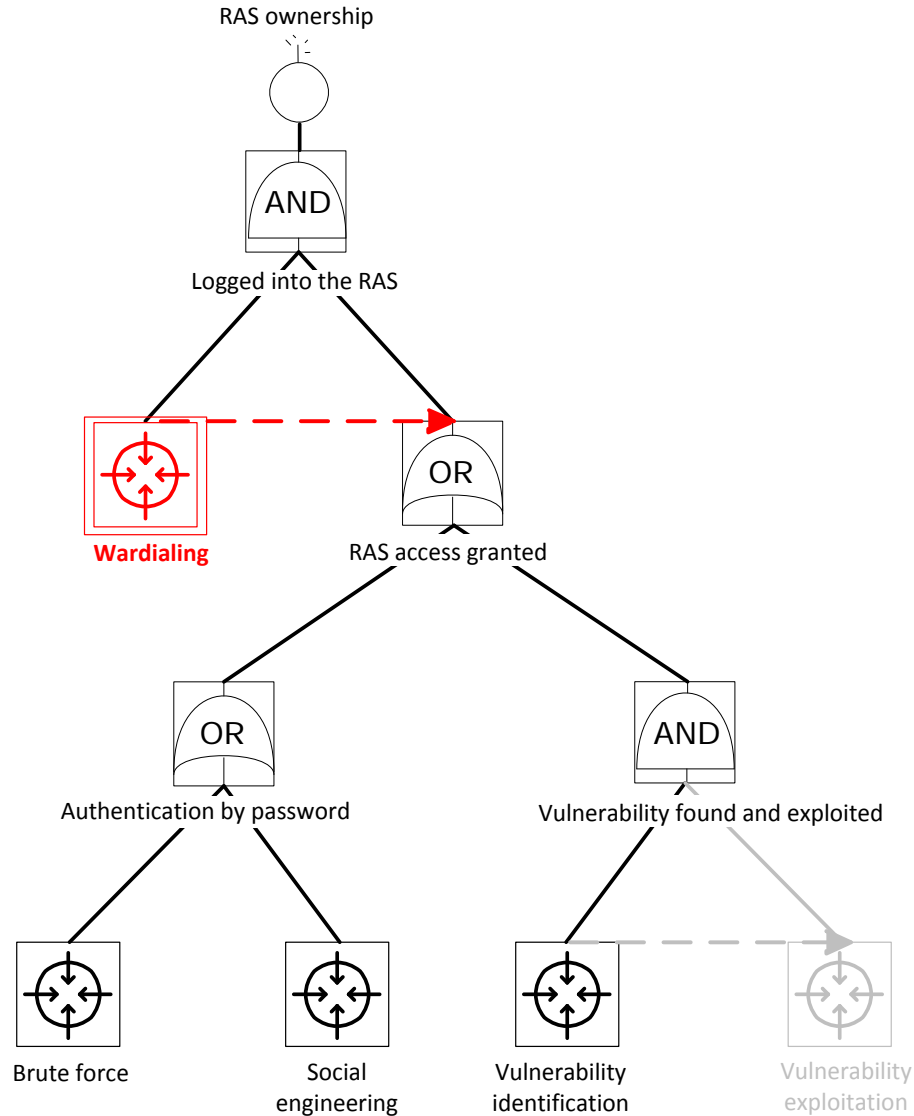




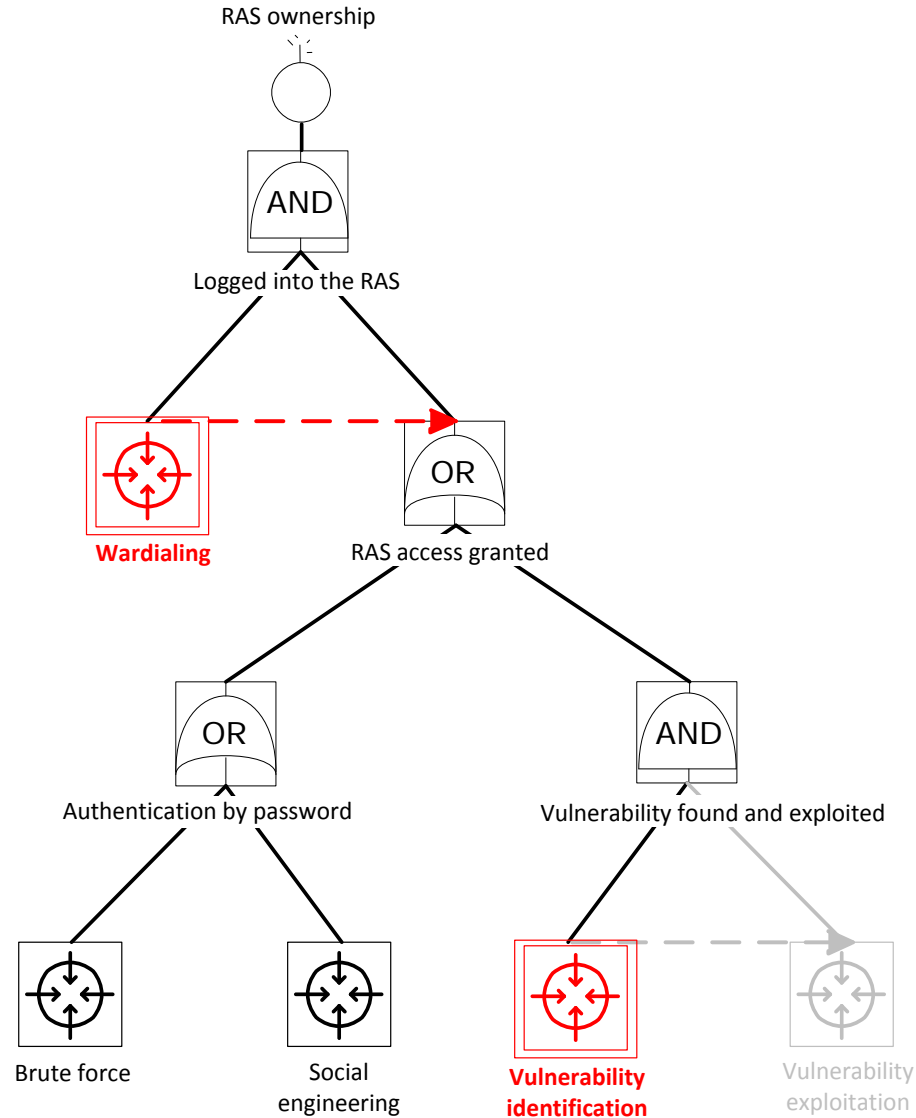
# RAS attack BDMP – Step 1



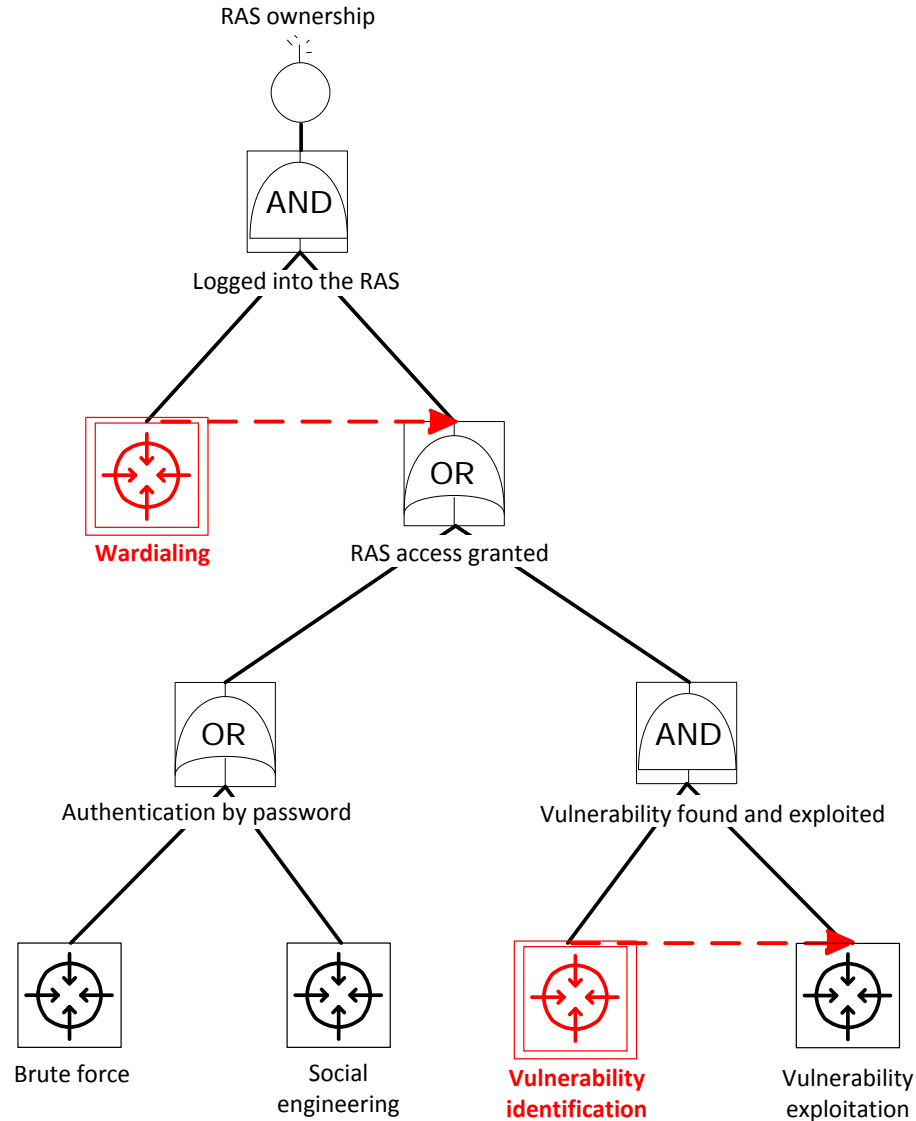
# RAS attack BDMP – Step 1



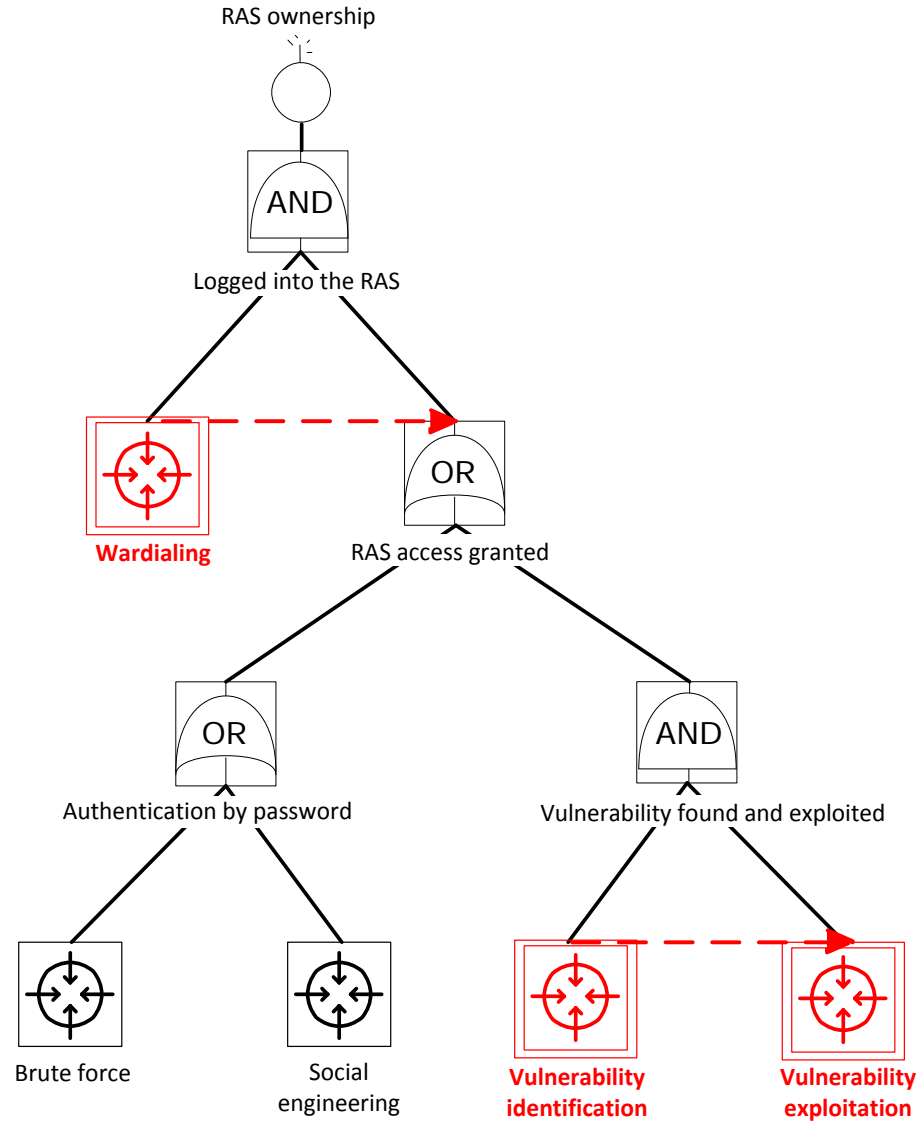
# RAS attack BDMP – Step 2



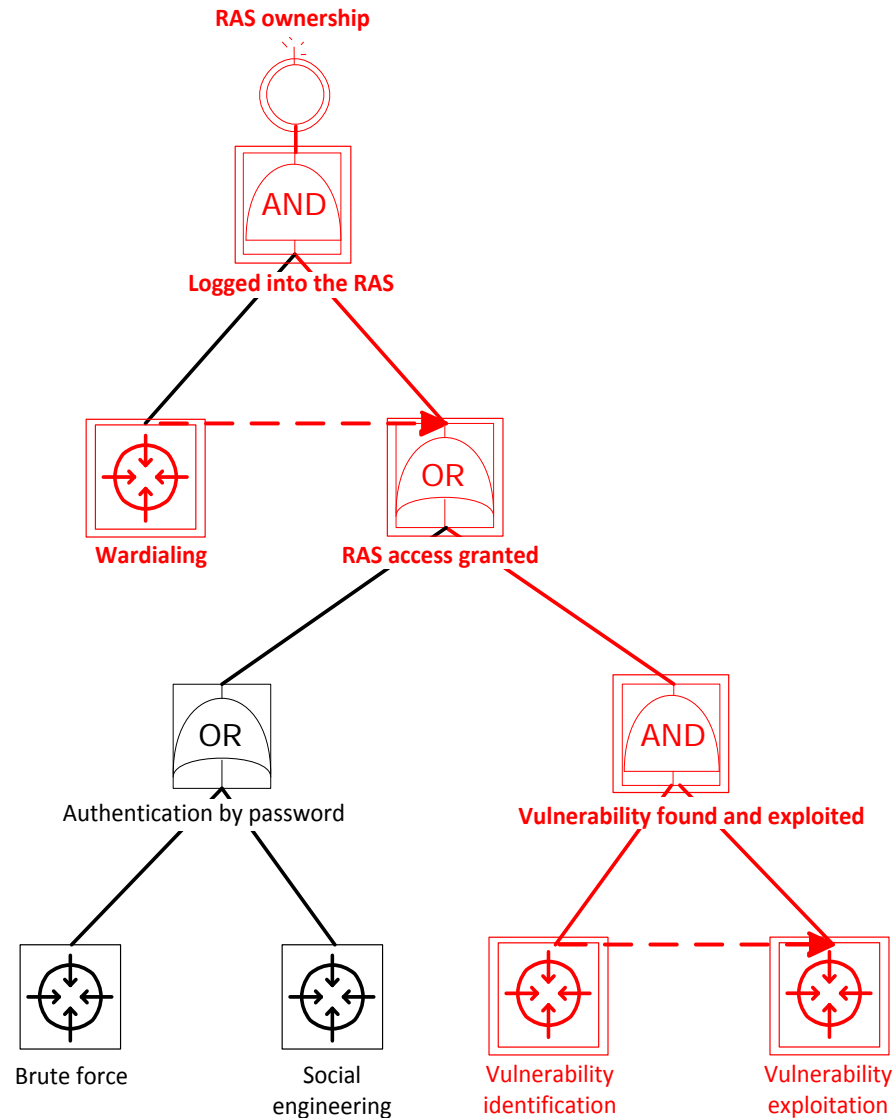
# RAS attack BDMP – Step 2



# RAS attack BDMP – Step 3



# RAS attack BDMP – Attacker's objective reached



# BDMP for attack modeling – Types of leaves

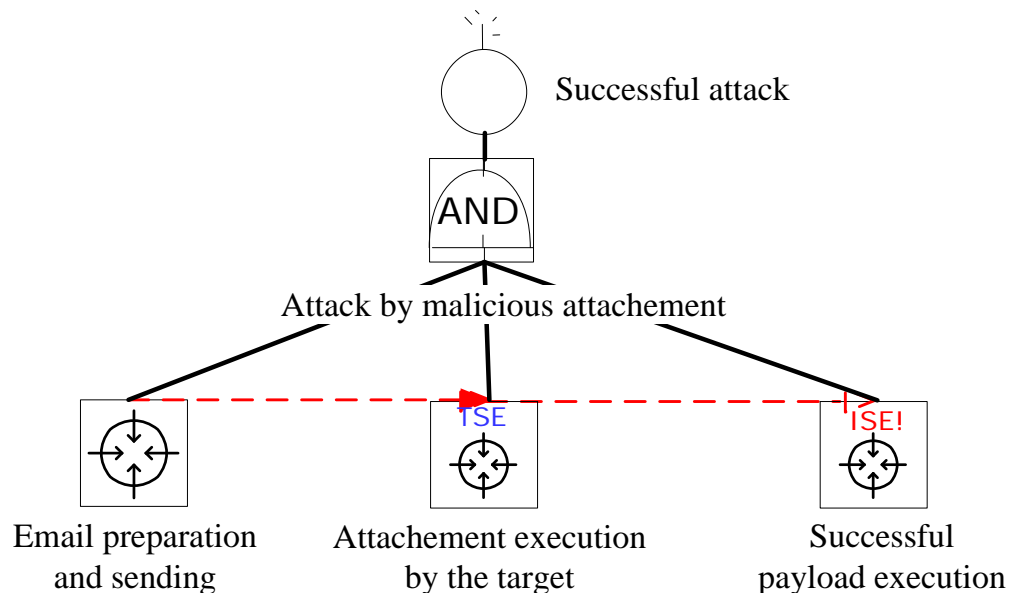
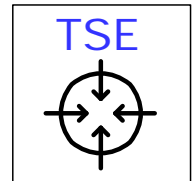
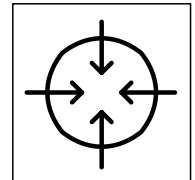
## ▶ Attack scenarios ⇒ 3 kinds of security leaves

### ■ Modeling of attacker's actions

- AA (*Attacker Action*) leaves, timed leaves ( $1/\lambda = \text{MTTS}$ )

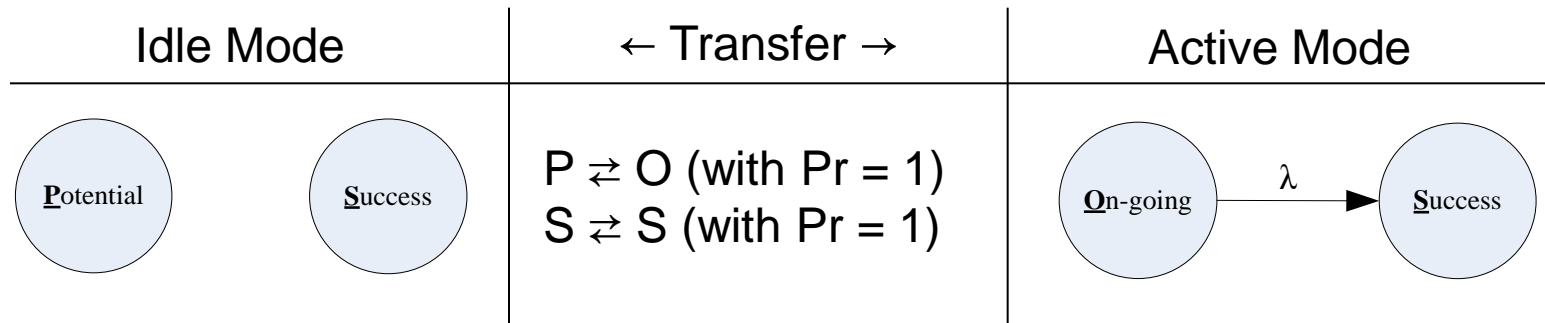
### ■ Modeling of security events

- TSE (*Timed Security Event*) leaves, timed as well
- ISE (*Instantaneous Security Event*) leaves, instantaneous ( $\gamma$ )



# BDMP for attack modeling – Going deeper

- ▶ Triggered Markov processes (e.g., AA leaf without detection)



- ▶ Leaf specifications for AA, ISE and TSE

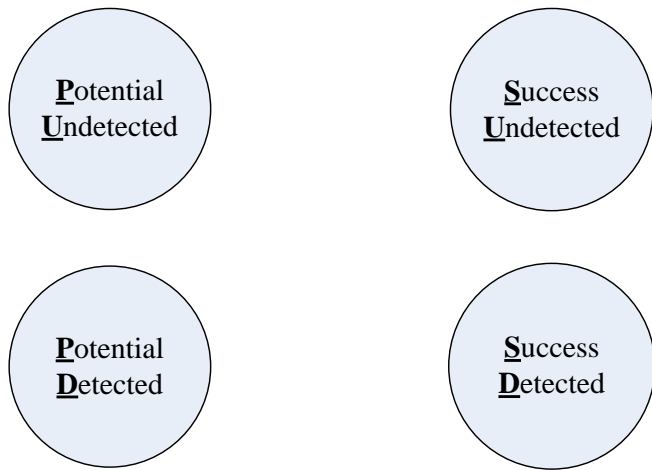
- ▶ Detection and reaction modeling

- Four types (IOFA): Initial, On-going, Final, A posteriori
- Three modes instead of two
  - Idle, Active Detected, and Active Undetected

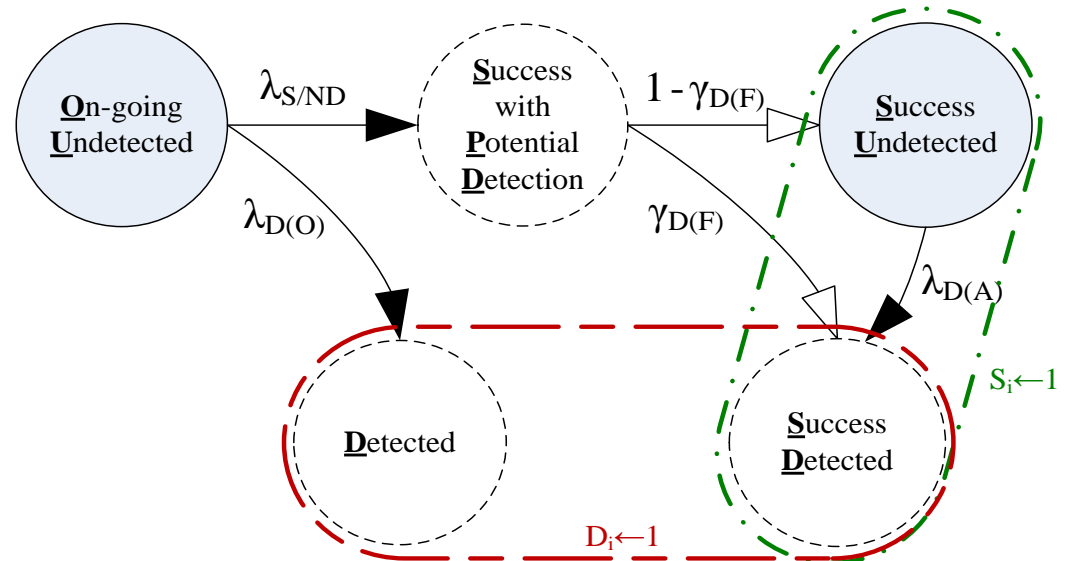


# Detections/reactions for AA leaves

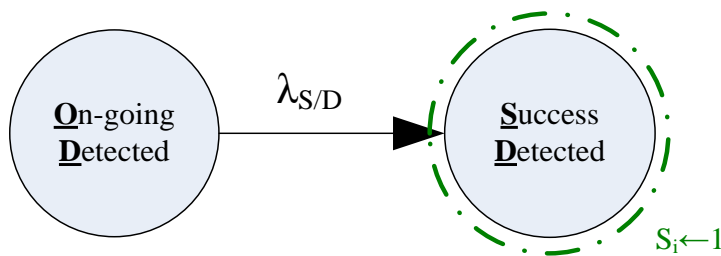
## Idle Mode



## Active Undetected Mode



## Active Detected Mode



## Transfer functions

$$f_{0 \rightarrow 10}^i(PU) = \{Pr(OU) = 1 - \gamma_{D(I)}, Pr(D) = \gamma_{D(I)}, Pr(SD) = 0, Pr(SU) = 0\}$$

$$(PD) = \{Pr(OU) = 0, Pr(D) = 1, Pr(SD) = 0, Pr(SU) = 0\}$$

$$(SU) = \{Pr(OU) = 0, Pr(D) = 0, Pr(SD) = 0, Pr(SU) = 1\}$$

$$(SD) = \{Pr(OU) = 0, Pr(D) = 0, Pr(SD) = 1, Pr(SU) = 0\}$$

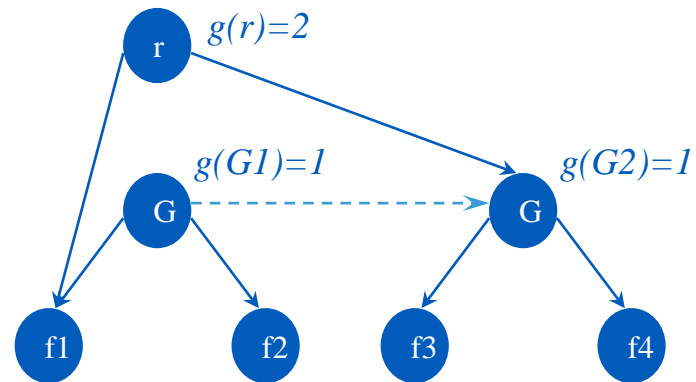
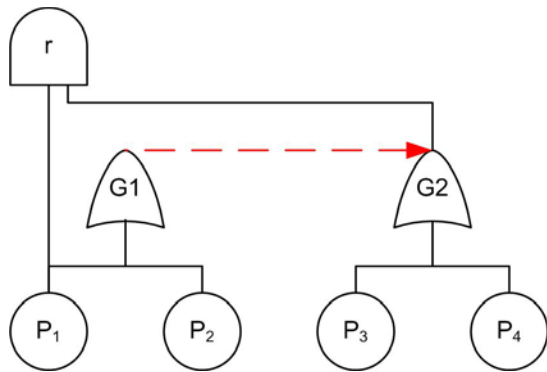
[...]

# Formal foundations – snapshot 1/3

A (security-oriented) BDMP  $(\mathcal{A}, r, T, P)$  is made of

► An attack tree  $\mathcal{A} = \{E, L, g\}$

- a set  $E = G \cup B$ , where  $G$  is a set of gates and  $B$  a set of basic events
- $(E, L)$  a directed acyclic graph, with  $L$  a set of oriented edges  $(i, j)$
- a function  $g$ , defining the gates ( $g:G \rightarrow N^*$ , with  $g(i)$  the gate parameter  $k$ )



► A main top objective  $r$

► Set of triggers  $T$  is a subset of  $(E - \{r\}) \times (E - \{r\})$  such that

$$\forall (i, j) \in T, i \neq j \text{ and } \forall (i, j) \in T, \forall (k, l) \in T, i \neq k \Rightarrow j \neq l$$

# Formal foundations – snapshot 2/3

## ▶ $P = \{P_i\}_{i \in E}$ , triggered Markov Processes

$$P_i = \left\{ Z_0^i(t), Z_{10}^i(t), Z_{11}^i(t), f_{0 \rightarrow 10}^i, f_{0 \rightarrow 11}^i, f_{10 \rightarrow 11}^i, f_{10 \rightarrow 0}^i, f_{11 \rightarrow 0}^i \right\}$$

### ■ $Z_0^i(t)$ , $Z_{10}^i(t)$ and $Z_{11}^i(t)$ three homogeneous Markov process

- For  $k$  in  $\{0, 1\}$  (modes),  $A_k^i$  state-space of  $Z_k^i(t)$
- $S_k^i \subset A_k^i$ , subset of successes/security event realizations
- $D_k^i \subset A_k^i$ , subset of detected states

### ■ $f_{0 \rightarrow 10}^i(x)$ [...] $f_{11 \rightarrow 0}^i(x)$ “probability transfer functions” with

- $\forall x \in A_0^i$ ,  $f_{0 \rightarrow 10}^i(x)$  is a probability distribution on  $A_{10}^i$  such that  $x \in S_{10}^i \Rightarrow \sum_{j \in S_{10}^i} (f_{0 \rightarrow 10}^i(x))(j) = 1$  and  $x \in D_{10}^i \Rightarrow \sum_{j \in D_{10}^i} (f_{0 \rightarrow 10}^i(x))(j) = 1$
- [...] x 5  $\left\{ f_{0 \rightarrow 11}^i, f_{10 \rightarrow 11}^i, f_{10 \rightarrow 0}^i, f_{11 \rightarrow 0}^i \right\}$

# Formal foundations – snapshot 3/3

## ► Four families of Boolean functions of the time

### ■ Structure functions $(S_i)_{i \in E}$

$$\forall i \in G, S_i \equiv \sum_{j \in \text{sons}(i)} S_j \geq g(i)$$

$$\forall j \in B, S_j \equiv Z_{X_j}^j \in S_{X_j}^j, \text{ with } X_j = 0 \text{ or } 1, \text{ indicating the mode in which } P_j \text{ is at time } t$$

### ■ Process selectors $(X_i)_{i \in E}$

If  $i$  is a root of  $\mathcal{A}$ , then  $X_i = 1$  else

$$X_i \equiv \neg \left[ \left( \forall x \in E, (x, i) \in L \Rightarrow X_x = 0 \right) \vee \left( \exists x \in E / (x, i) \in T \wedge S_x = 0 \right) \right]$$

### ■ Relevance indicators $(Y_i)_{i \in E}$

If  $i = r$  (final objective), then  $X_i = 1$  else

$$Y_i \equiv \left( \exists x \in E / (x, i) \in L \wedge Y_x \wedge S_x = 0 \right) \vee \left( \exists y \in E / (i, y) \in T \wedge S_y = 0 \right)$$

### ■ Detection status indicators $(D_i)_{i \in E}$

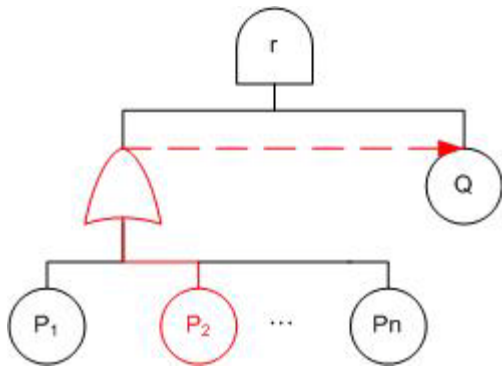
$$\forall i \in B, D_i \equiv \left( Z_{X_i}^i \in D_{X_i}^i \right) \vee \left( \exists j \in B / j \neq i \wedge D_j = 1 \right) \quad \forall j \in G, D_j \equiv \left( \exists i \in B / D_i = 1 \right)$$

# Mathematical properties

## ▶ Robustness

- **Theorem 1:**  $(S_i)(X_i)(Y_i)(D_{i \in E})$  are computable whatever the BDMP structure
- **Theorem 2 :** Any BDMP, defined at time  $t$  by the modes and the  $P_i$  states, is a valid homogeneous Markov process

## ▶ Combinatory reduction by “relevant event filtering”



- After attack step  $P_2$ , all the others  $P_i$  are not relevant anymore: nothing is changed for “r” if we inhibit them
- The number of sequences leading to the top objective is
  - n, if we filter the relevant events  $(\{P_1, Q\}, \{P_2, Q\}, \dots)$
  - exponential otherwise  $(\{P_1, Q\}, \{P_1, P_2, Q\}, \{P_1, P_3, Q\}, \dots)$

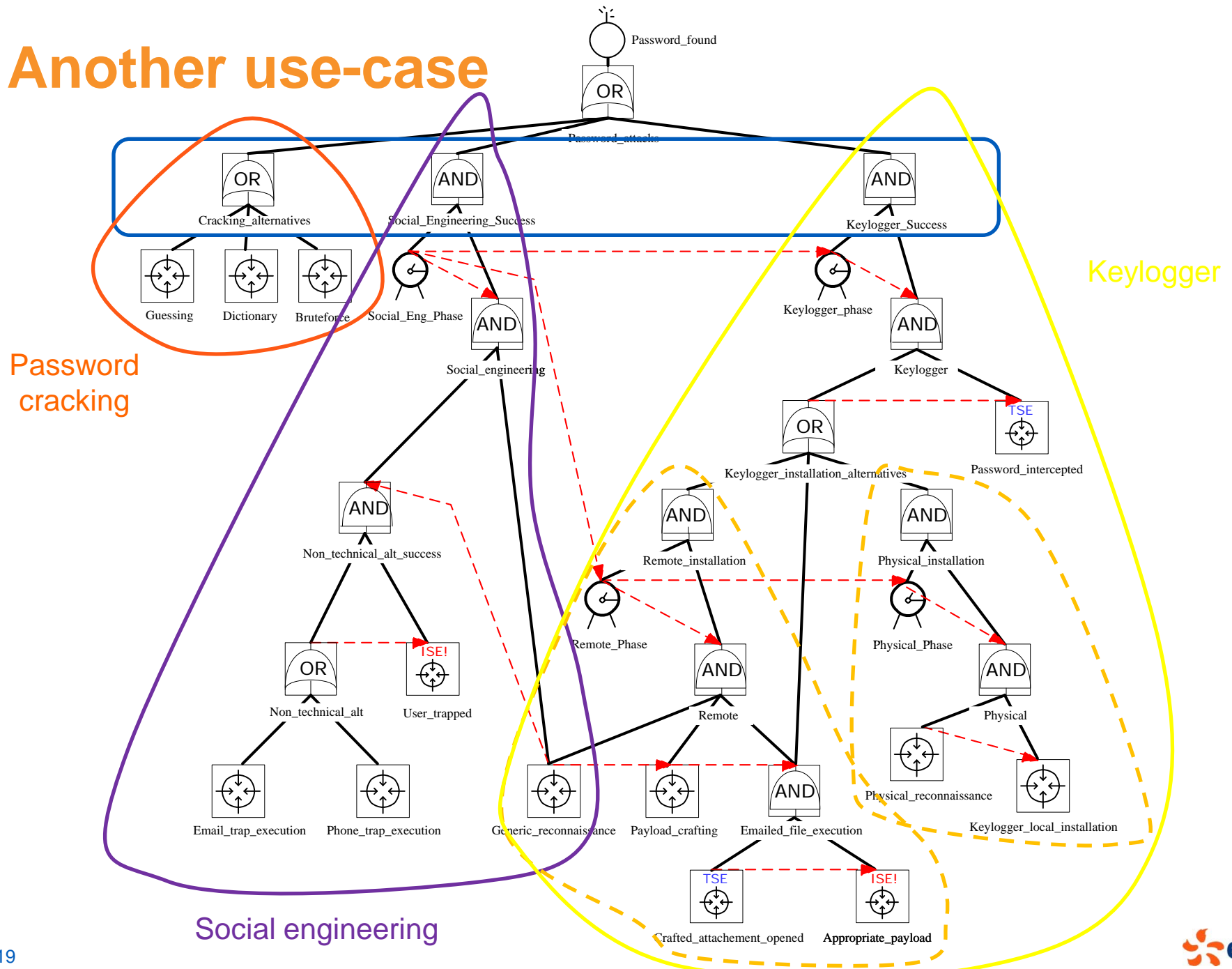
- **Theorem 3:** if the  $P_i$  are such that  $\forall i \in B, \forall t, \forall t' \geq t, S_i(t) = 1 \Rightarrow S_i(t') = 1^*$  and detection aspects are not considered,  $Pr(S_r(t)=1)$  is unchanged whether irrelevant event  $(Y_i=0)$  are trimmed or not.

\* This is always the case in our framework

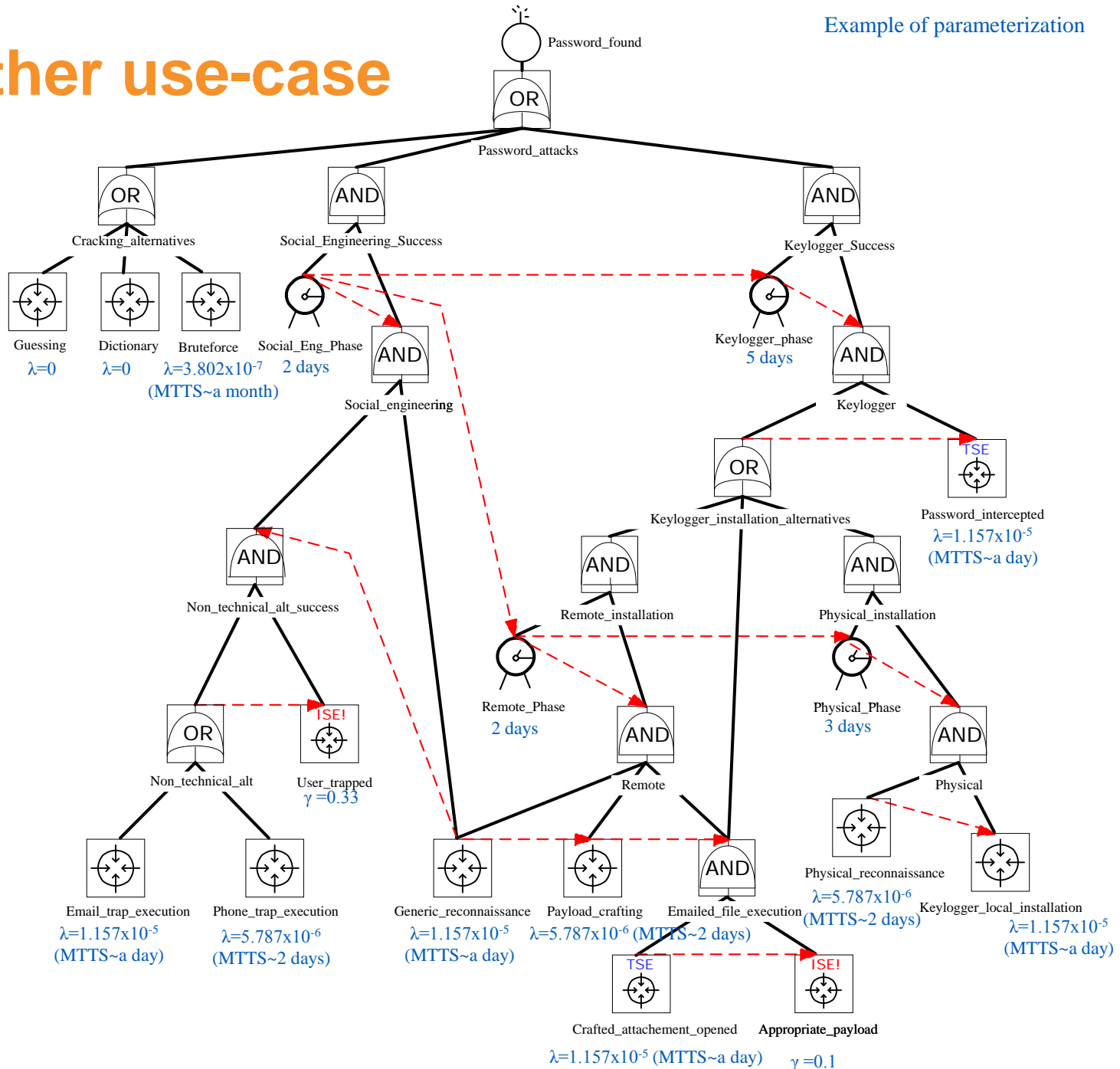
# Quantifications

- ▶ **Time-independent (static) - Classical attack tree parameters**
  - Monetary cost → scenario cost, average attack cost
  - Boolean indicators (specific requirements, properties)
  - Minimum attacker skills
  
- ▶ **Time-domain analysis – Leveraging the BDMP framework**
  - Quantification tools, algorithms and optimizations
  - Efficient sequence exploration with trimming
    - Probability to reach the objective in a given time
    - Overall mean time to the attack success
    - Probability of each explored sequence
    - Ordered list of sequences

# Another use-case



# Another use-case





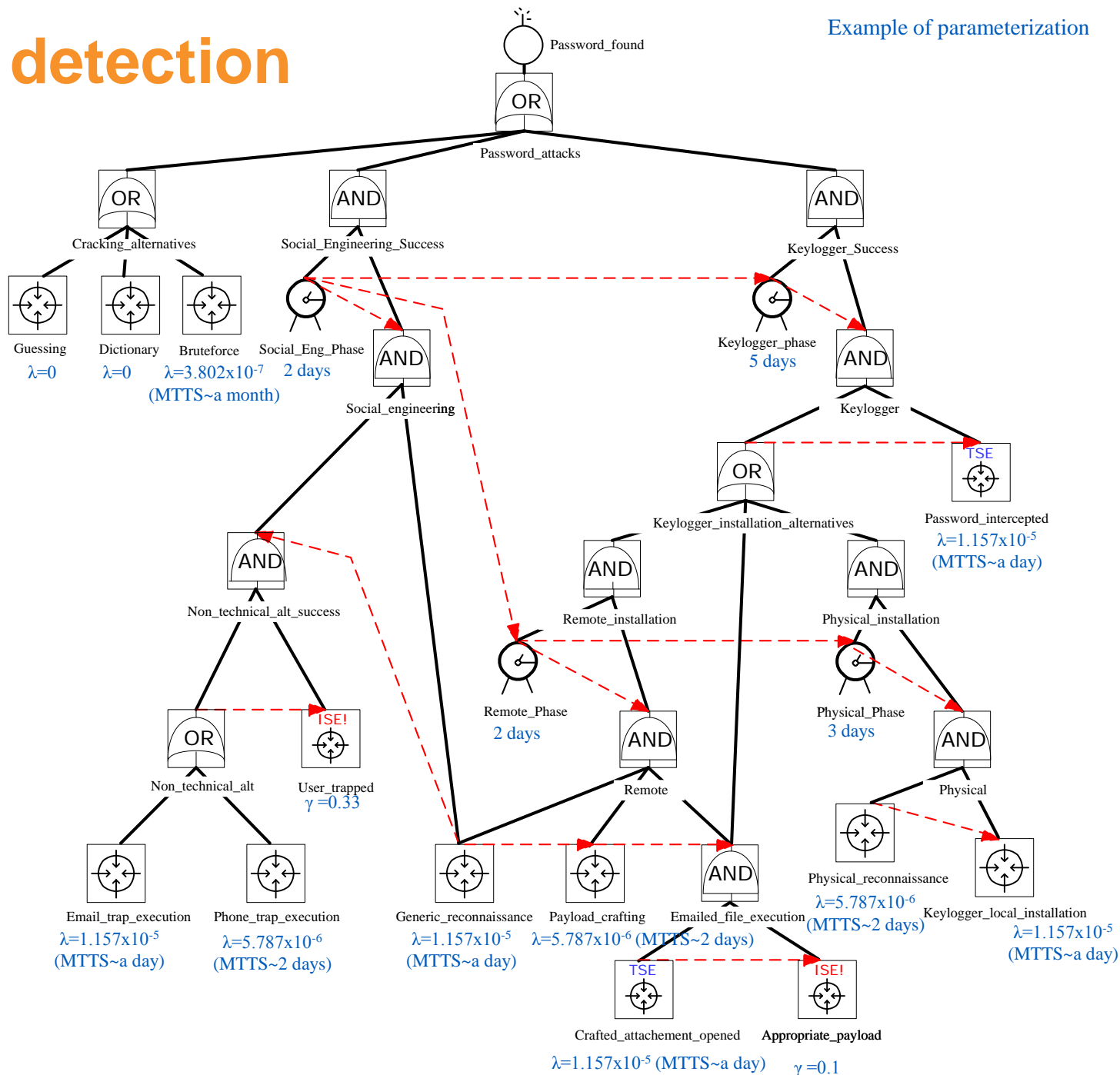
# Results

- Overall probability in a week = 0.422 (MTTS = 22 days)
- Ordered list of attack sequences (654 sequences)

|     | Sequences   | Probability in a week  | Average duration    | Contrib. |
|-----|---|------------------------|---------------------|----------|
| 1   | <Social Eng>Generic reconn., Email trap exec., User trapped   | $1.059 \times 10^{-1}$ | $9.889 \times 10^4$ | 25.1%    |
| 2   | <Social Eng>Generic reconn., Phone trap exec., User trapped   | $5.295 \times 10^{-2}$ | $9.889 \times 10^4$ | 12.5%    |
| 3   | Bruteforce  | $2.144 \times 10^{-2}$ | $5.638 \times 10^4$ | 5.1%     |
| 4   | <Social Eng></Social Eng><Keylogger><Remote></Remote><Physical> Physical reconn., Keylogger local installation, Password intercepted  | $1.749 \times 10^{-2}$ | $2.976 \times 10^5$ | 4.1%     |
| 5   | <Social Eng></Social Eng><Keylogger> <Remote>Generic reconnaissance </Remote><Physical>Physical reconnaissance, Keylogger local installation, Password intercepted  | $1.350 \times 10^{-2}$ | $3.677 \times 10^5$ | 3.2%     |
| 6   | <Social Eng>Generic reconnaissance, Email trap execution, User trapped(failure), Bruteforce   | $1.259 \times 10^{-2}$ | $2.610 \times 10^5$ | 3.0%     |
| ... |   |                        |                     |          |
| 20  | <Social Eng></Social Eng><Keylogger><Remote>Generic reconnaissance, Payload crafting, Appropriate payload, Password intercepted   | $2.500 \times 10^{-3}$ | $2.761 \times 10^5$ | 0.6%     |
| ... |   |                        |                     |          |
| 34  | <Social Eng></Social Eng><Keylogger> <Remote>Generic reconn., Payload crafting </Remote> <Physical>Crafted attachment opened, Appropriate payload, Physical reconn., Keylogger local installation, Password intercepted | $1.506 \times 10^{-3}$ | $4.594 \times 10^5$ | 0.4%     |

# With detection

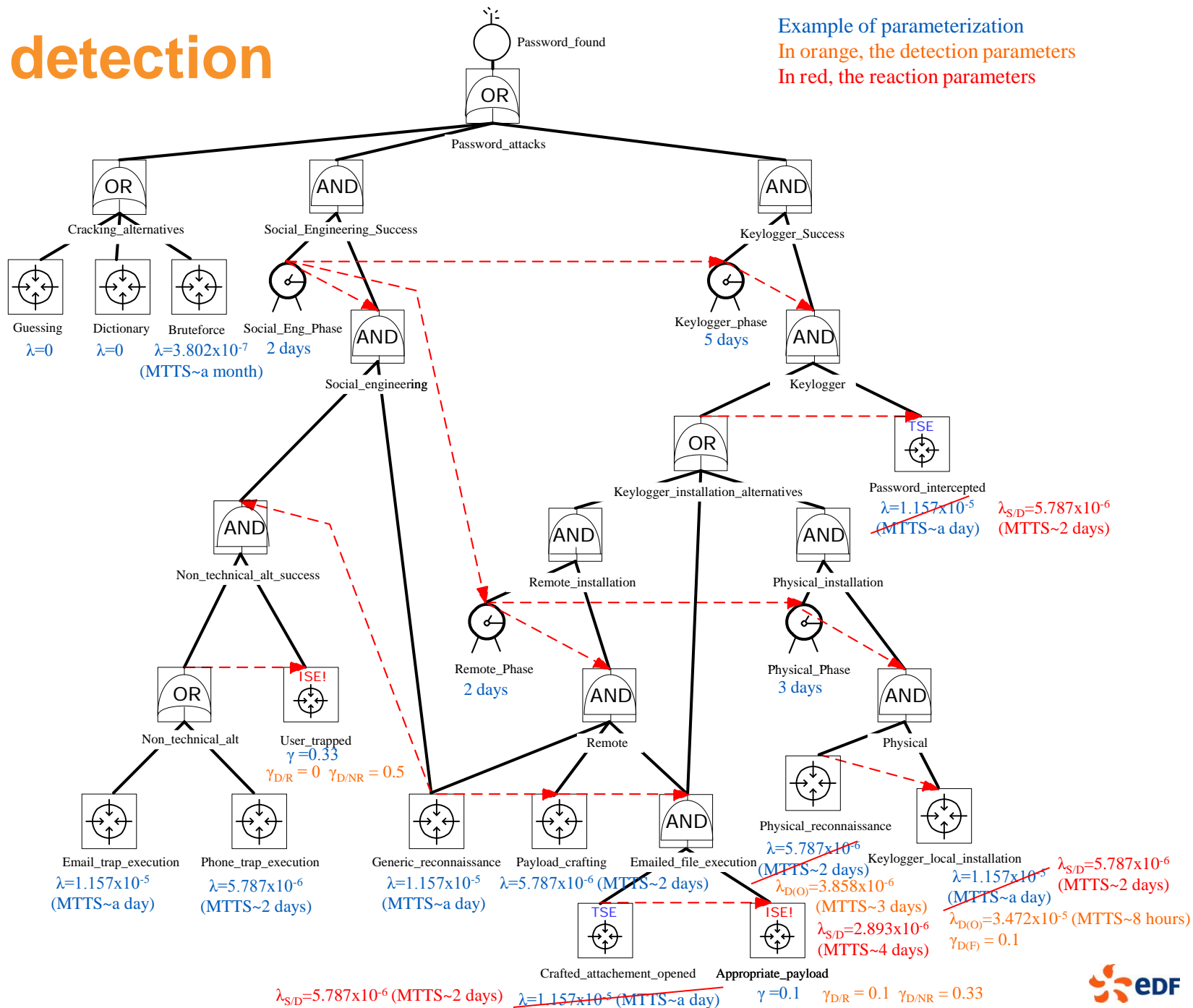
Example of parameterization





# With detection

Example of parameterization  
 In orange, the detection parameters  
 In red, the reaction parameters



# Results

- Probability of success within a week = 0.364 (-14 %)
- Representative sequences (4231 vs 654)

|     | Sequences  | Probability in a week  | Average duration    | Contrib. |
|-----|--|------------------------|---------------------|----------|
| 1   | <Social Eng>Generic reconn., Email trap exec., User trapped  | $1.091 \times 10^{-1}$ | $9.889 \times 10^4$ | 30.0%    |
| 2   | <Social Eng>Generic reconn., Phone trap exec., User trapped  | $5.456 \times 10^{-2}$ | $9.889 \times 10^4$ | 15.0%    |
| 3   | Bruteforce   | $2.144 \times 10^{-2}$ | $5.638 \times 10^4$ | 5.9%     |
| 4   | <Social Eng> <i>Generic reconnaissance</i> , Bruteforce  | $1.055 \times 10^{-2}$ | $9.889 \times 10^4$ | 2.9%     |
| ... | ([...], Bruteforce) × 9  |                        |                     |          |
| 14  | <Social Eng><Social Eng><Keylogger><Remote>Generic reconnaissance, Payload crafting(no detection), Appropriate payload(no detection), Password intercepted   | $2.250 \times 10^{-3}$ | $2.761 \times 10^5$ | 0.6%     |
| ... | ([...], Bruteforce) × 2  |                        |                     |          |
| 17  | <Social Eng>Generic reconnaissance <Social Eng><Keylogger><Remote>Payload crafting(no detection), Appropriate payload(no detection), Password intercepted  | $1.923 \times 10^{-3}$ | $2.688 \times 10^5$ | 0.5%     |
| ... | ([...], Bruteforce) × 2  |                        |                     |          |
| 20  | <Social Eng> <i>Generic reconnaissance, Email trap exec., User trapped(failure and detection)</i> <Social Eng><Keylogger><Remote><Remote> <Physical>Physical reconn., Keylogger local installation, Password intercepted | $1.549 \times 10^{-3}$ | $5.991 \times 10^5$ | 0.4%     |

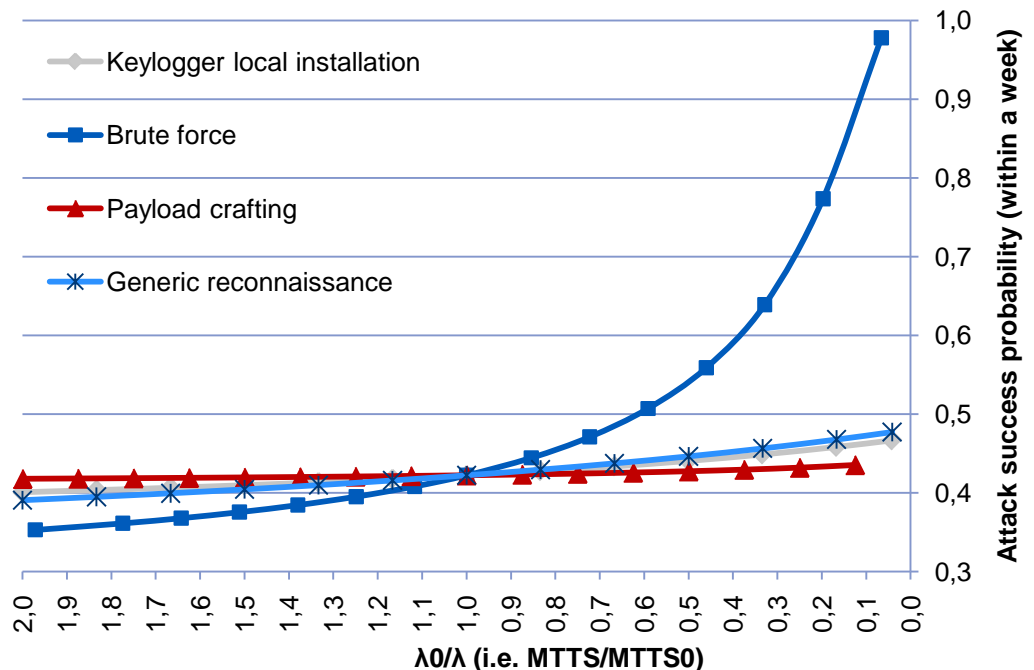
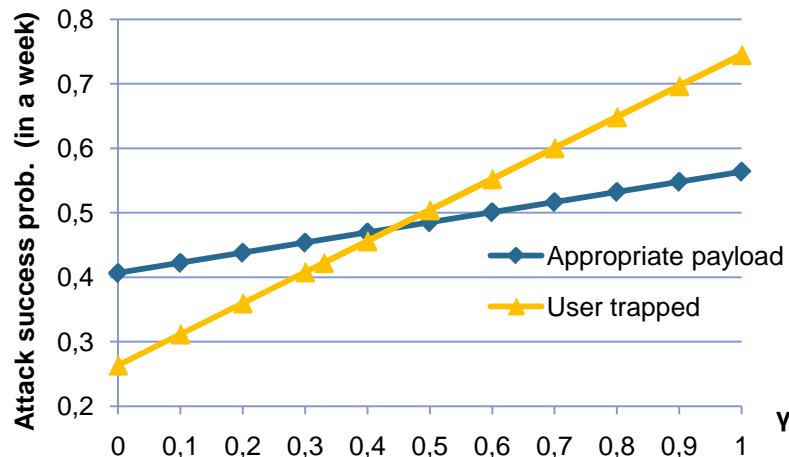
# Recent enhancements & complementary tools

## Sequence analysis

- Filtering by static/time-independent parameters, i.e. attacker profile
- Sequence presentation (visual conventions)

## Sensitivity analysis

- Optimize security efforts
- Most “significant” leaves
- Iterated treatments

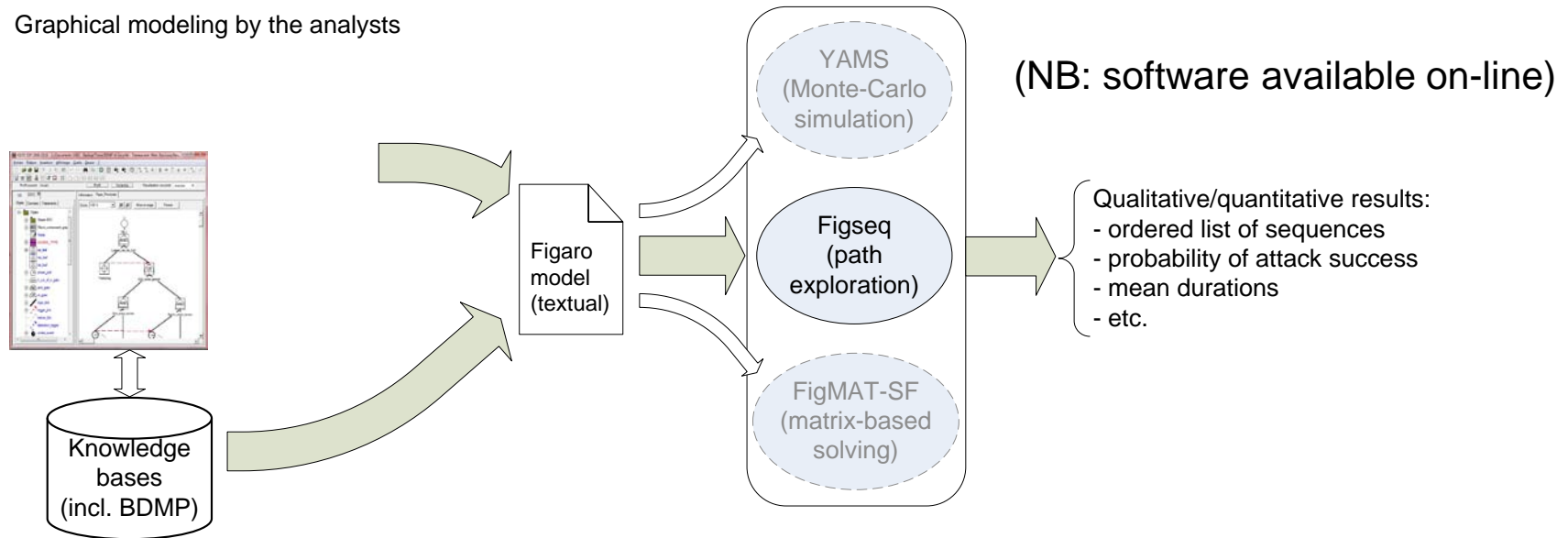


# A few words about the implementation

## ▶ Leveraging of the KB3 platform (EDF)

- Used at EDF for dependability studies for more than 15 years
- Modularity thanks to “Knowledge Bases”, written in Figaro

Graphical modeling by the analysts



## ▶ A dedicated security knowledge basis

- Implementation was easy and fast (available on-line)

# Perspectives and on-going work

## ▶ Enhance usability

- Users' feedback, case-studies, tutorials
- Side-tools (sensitivity script HMI, etc.)
- Attack pattern library

## ▶ Theoretical extensions

- Experiment different probability distributions (e.g., McQueen *et al.*)
- Integration with Bayesian networks
- Many attack trees extensions could be adapted
  - Intervals, fuzzy sets, OWA gates, game theory, etc.
- Uncertainty handling and propagation

## ▶ Internal and external dissemination! (thanks 😊)



# Conclusion

## ▶ Graphical security modeling

- Different balances between readability, scalability, modeling power and quantification capabilities

## ▶ BDMP, an original and attractive trade-off

- With a sound theoretical framework
- Already an operational formalism

## ▶ Limits

- Inherent limits of BDMP (e.g., with cyclic behaviors/loops)
- Attacker behavior stochastic modeling – subjective probabilities
- More generally, security and quantitative assessments
- Complementary tool for the security analyst

# Some references

## ▶ On BDMP & KB3

- M. Bouissou, J.L. Bon, "A new formalism that combines advantages of fault-trees and Markov models: Boolean logic Driven Markov Processes," *Reliability Engineering and System Safety*, Vol. 82, Issue 2, nov. 2003, pp. 149-163
- M. Bouissou, "Automated Dependability Analysis of Complex Systems with the KB3 Workbench: the Experience of EDF R&D," *Proceedings of CIEM 2005*, Bucharest, Romania, oct. 2005

Marc Bouissou's homepage: <http://marc.bouissou.free.fr/>

## ▶ On BDMP & Security

- L. Piètre-Cambacédès et M. Bouissou, "Attack and defense dynamic modeling with BDMP," in *Proc. 5th International Conference on Mathematical Methods, Models, and Architectures for Computer Networks Security (MMM-ACNS-2010)*, St Petersburg, Russia, sept. 2010
- L. Pietre-Cambacedes, Y. Deflesselle and M. Bouissou, "Security modeling with BDMP: from theory to implementation," in *Proc. 6th IEEE International Conference on Network and Information Systems Security (SAR-SSI 2011)*, La Rochelle, France, may 2011
- L. Piètre-Cambacédès and M. Bouissou, "Modeling safety and security interdependencies with BDMP (Boolean logic Driven Markov Processes)," *Proc. IEEE International Conference on Systems, Man, and Cybernetics (SMC 2010)*, Istanbul, Turkey, oct. 2010.

Ludovic Pietre-Cambacedes' homepage: <http://perso.telecom-paristech.fr/~pietrec/>

Try the tools:  
Free download on Sourceforge/Visualfigaro  
(or look for « KB3 EDF » in Google)

**THANK YOU VERY MUCH!**