

Specification of the Transit Node in PSF_d

S. Mauw F. Wiedijk

University of Amsterdam
Programming Research Group
P.O.Box 41882, 1009 DB Amsterdam
The Netherlands

abstract The specification language PSF_d is used to give a formal specification of a transit node, a common case study in ESPRIT project METEOR. The design of the specification derived from the informal text and the ERAE specification is included. A short discussion on the relation to the specification in ERAE is provided.

1. INTRODUCTION

This paper contains a case study in the formal description technique PSF_d . We specify a transit node, which is the common case study for several formalisms in the ESPRIT project METEOR. In [MHB89] the transit node is specified in the algebraic specification language PLUSS. The PSF_d specification is derived partially from an informal text and partially from the ERAE specification in [Hag88]. The design of the specification is included, from which a general method can be derived for specifying similar problems in PSF_d .

In [MHB89] the transit node is specified in the algebraic specification language PLUSS.

The PSF_d specification can be viewed at as a more implementation directed specification than the one in ERAE. Certain design decisions are made, e.g. in identifying the separate objects that act in parallel. Thus the PSF_d specification, viewed as an implementation of the ERAE specification must be verified or validated. A short discussion is devoted to this topic.

2. PSF_d

PSF_d (Process Specification Formalism - Draft) is a Formal Description Technique developed for specifying concurrent systems. The formal definition of PSF_d can be found in [MV88]. In [MV89] an introduction to the basic features is given.

PSF_d has been designed as the base for a set of tools to support ACP (Algebra of Communicating Processes) [BK86]. We use bisimulation semantics to attach a meaning to the specification of processes. The part of PSF_d that deals with the description of the data is based on ASF (Algebraic Specification Language) [BHK89]. Here we use initial algebra semantics.

PSF_d supports the modular construction of specification and parameterization of modules.

3. THE TRANSIT NODE

The Transit Node is a case study, which was defined in the RACE project 1046 (SPECS). An informal description of the Transit Node and the ERAE specification of it can be found in [Hag88]. The informal specification reads as follows:

"The system to be specified consists of a transit node with:

- 1 Control Port-In*
- 1 Control Port-Out*
- N Data Ports-In*
- N Data Ports-Out*
- M Routes Through*

(The limits of N and M are not specified.)

Each port is serialized. All ports are concurrent to all others. The ports should be specified as separate, concurrent entities. Messages arrive from the environment only when a Port-In is able to treat them.

The node is "fair". All messages are equally likely to be treated, when a selection must be made, and all messages will eventually transit the node, or be placed in the collection of faulty messages.

Initial State: 1 Control Port-In, 1 Control Port-Out.

The Control Port-In accepts and treats the following three messages:

- Add-Data-Port-In-&-Out(n)*
gives the node knowledge of a new port-in(n) and a new port-out(n). The node commences to accept and treat messages sent to the port-in, as indicated below on Data Port-In.
- Add-Route((m),n(i),n(j),...))*
gives the node knowledge of a route associating route m with Data Port-Out(n(i),n(j),...).
- Send-Faults*
routes all saved faulty messages, if any to Control-Port-Out. The order in which the faulty messages are transmitted is not specified.

A Data Port-In accepts and treats only messages of the type:

- Route(m).Data*
The Port-In routes the message, unchanged, to any one (non-determinate) of the Data Ports-Out associated with route m. (Note that a Data Port-Out is serialized - the message has to be buffered until the Data Port-Out can process it). The message becomes a faulty message if its transit time through the node (from initial receipt by a Data Port-In to transmission by a Data Port-Out) is greater than a constant time T.

Data Ports-Out and Control Port-Out accept messages of any type and will transmit the message out of the node. Messages may leave the node in any order.

All faulty messages are saved until a Send-Faults command message causes them to be routed to Control Port-Out. Faulty messages are messages on the Control Port-In that are not one of the three commands listed, messages on a Data Port-In that indicate an unknown route, or messages whose transit time through the node is greater than T. Messages that exceed the transit time of T become faulty as soon as the time T is exceeded. It is permissible for a faulty message to not be routed to Control Port-Out (because, for example, it has just become faulty, but has not yet been placed in a faulty message collection), but all faulty messages must eventually be sent to Control Port-Out with a succession of Send-Faults commands.

It may be assumed that a source of time (time-of-day or a signal each time interval) is available in the environment and need not be modeled with the specification."

4. DESIGN OF THE SPECIFICATION

4.1. General

The specification was designed using a mixed top-down and bottom-up approach. It was based on the informal text, while using the interpretation of the text in the ERAE specification when needed to fill in omissions or solve ambiguities.

Several design decisions were made, which did not follow directly from the informal description of the case study. (e.g. the decision to let the Control Port-in keep control of the table containing all routes through the node).

4.2. Design

We first identify all parameters of the system, i.e. objects which are -and should be- unspecified. Since "it may be assumed that a source of time is available in the environment", we postulate the existence of a process that behaves like a *clock*. This can be done by making a parameter containing this *clock* process. The second parameter is formed by the time that a message may be inside the node without getting faulty, the *maximal transit time*. The exact length of this duration should be decided upon at the implementation phase.

Then we identify all (concurrent) components in the system. We have a *Control-Port-In*, a *Control-Port-Out*, a number of *Data-Ports-in* and a number of *Data-Ports-Out*. Note that we don't consider the *Routes* as components, since these are static objects without temporal behaviour. Because all *Data-Ports-In* have the same behaviour, we can specify just one process, indexed with the actual name of the port. The same holds for the *Data-Ports Out*.

Now we make the decision that the routes and the information about the ports that exist are handled by the *Control-Port-In*, so this process is indexed with a *route-table* and with a *port-set*. Furthermore we see that the *Control-Port-Out* must contain a number of faulty messages that should be flushed and that every *Data-Port-Out* must contain a number of messages that should be sent to the environment. So both processes are indexed with a *message-bag*. The signature of the top-level objects now looks like:

```
processes
control-port-in : route-table # port-set
control-port-out : message-bag
data-port-in : port-name
data-port-out : port-name # message-bag
```

From the informal text and the ERAE specification we can now define the initial state of the the node. It consists of the concurrent operation of the *control-port-in* and the *control-port-out*, indexed with the *empty-route-table*, the *empty-port-set* and the *empty-message-bag*. Of course we must add the parameter process *clock* in parallel and we must abstract from the internal actions and encapsulate unsuccessful communications.

```
transit-node = hide(I, encaps(H,
    clock ||
    control-port-in(empty-route-table, empty-port-set) ||
    control-port-out(empty-message-bag)))
```

Now we can proceed in a bottom up way by defining the data types *route-table* (an instance of the parameterized module *table* with the data type *routes*), *port-set* (sets instantiated with *ports*), *message-bag* (bags instantiated with *messages*) and *port-name*.

The top-down approach is continued by defining the behaviour of the four processes, each in a separate module. This leads to the question which objects are connected, in order to communicate to each other. We see that there is a link between the *control-port-in* and the *control-port-out*. Every *data-port-in* is linked to the *control-port-in* for route information and to the *control-port-out* for sending faulty messages. All *data-ports-in* are connected to all *data-ports-out* to transmit messages. And finally all ports have a connection to the environment for either accepting or transmitting messages.

As can be seen in the specification, the behaviour of the objects is specified by determining all initial communication actions. Every action is then followed by the corresponding behaviour, e.g. a transmission or a state change. This can possibly be specified by using subprocesses.

The *control-port-in* e.g. can accept one of the following messages:

- *add-datum-port(p)*, followed by the subprocess that handles adding a *data-port-in* and a *data-port-out*;
- *add-route(r)*, followed by a state change where the *route-table* is updated;
- *send-faults*, followed by forwarding this message to *control-port-out*;
- *request-route(rn)*, followed by sending appropriate information about the route back.

After having identified all atomic actions (i.e. communication attempts) we can define the communication function and the set of atoms that has to be encapsulated and abstracted.

4.3. Topology of the transit node

We can visualize the structure of the transit node with the following picture.

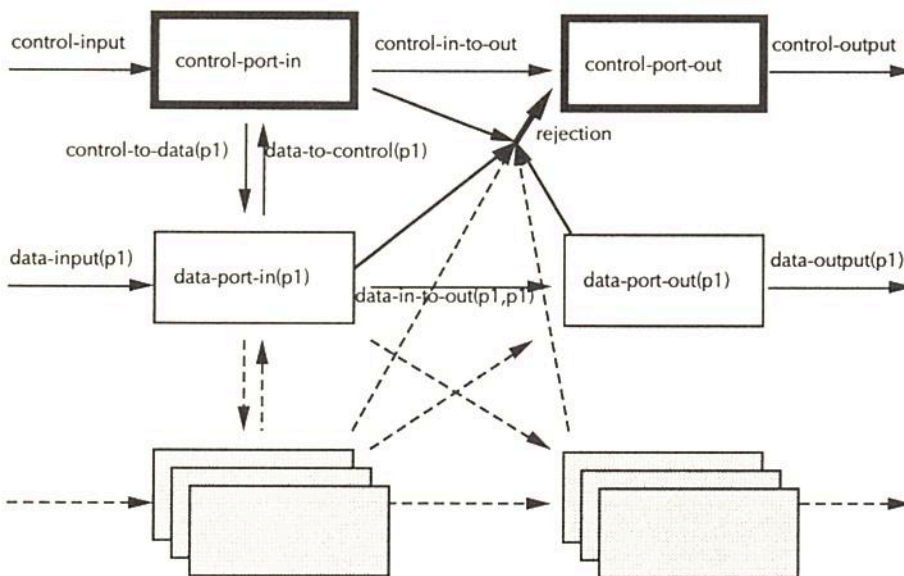


figure 1 The transit node

5. THE SPECIFICATION

The specification that resulted from the design as described in the previous paragraph will now be given. Note that the linear structure of the specification does not comply with the way the specification was designed. This is because the formalism forces us to write down the specification in a bottom-up way.

We first give all basic data types needed in the specification, then we define the data types specific to the transit node, then we define all processes involved and finally we give an example of an instantiation of the clock parameter.

5.1. Basic data types

The basic data types consist of the simple types *booleans* and *natural numbers*, and the parameterized types *bags*, *sets* and *tables*. The difference between bags and sets is that in a set duplicates are removed. A table can be used to look up an item corresponding to the value of a certain key.

```
data module booleans
begin
  exports
  begin
    sorts BOOL
    functions
      true  :          -> BOOL
      false :          -> BOOL
      or    : BOOL # BOOL -> BOOL
      and   : BOOL # BOOL -> BOOL
  end

  variables
    b : -> BOOL
  equations
    [1] or(true, b)  = true
    [2] or(false, b) = b
    [3] and(true, b) = b
    [4] and(false, b) = false
end

end booleans
```

```
data module natural-numbers
begin
  exports
  begin
    sorts nat
    functions
      0      :          -> nat
      s      : nat      -> nat
      eq     : nat # nat -> BOOL
      lt     : nat # nat -> BOOL
      _ + _  : nat # nat -> nat
      _ - _  : nat # nat -> nat
  end

  imports booleans
```



```

variables
  n, n1, n2 : -> nat
equations
  [1] eq(0, 0)           = true
  [2] eq(0, s(n))       = false
  [3] eq(s(n), 0)       = false
  [4] eq(s(n1), s(n2))  = eq(n1, n2)
  [5] lt(0, s(n))       = true
  [6] lt(n, 0)          = false
  [7] lt(s(n1), s(n2))  = lt(n1, n2)
  [8] n + 0              = n
  [9] n1 + s(n2)         = s(n1 + n2)
  [10] 0 - n             = 0
  [11] n - 0             = n
  [12] s(n1) - s(n2)    = n1 - n2

end natural-numbers

data module bags
begin

  parameters
    items
      begin
        sorts item
      end items

  exports
    begin
      sorts bag
      functions
        empty-bag : -> bag
        add       : item # bag -> bag
      end

  variables
    i1, i2 : -> item
    b       : -> bag
  equations
    [1] add(i1, add(i2, b)) = add(i2, add(i1, b))

end bags

data module set
begin

  parameters
    equality
      begin
        functions
          eq : item # item -> BOOL
        end equality

  exports
    begin
      functions
        eq       : set # set -> BOOL
        element : item # set -> BOOL
      end

end

```

```

imports
  bags
    { renamed by
      [ bag      -> set,
        empty-bag -> empty-set]
    },
  booleans
variables
  i, i1, i2 : -> item
  s         : -> set
equations
  [1] add(i, add(i, s))      = add(i, s)
  [2] element(i, empty-set) = false
  [3] element(i1, add(i2, s)) = or(eq(i1, i2), element(i1, s))
end set

data module tables
begin

  parameters
    items
      begin
        sorts key, value
        functions
          eq      : key # key -> BOOL
          default-value :      -> value
        end items

  exports
    begin
      sorts table
      functions
        empty-table :      -> table
        add         : key # value # table -> table
        look-up     : key # table   -> value
      end

  imports booleans

  variables
    k, k1, k2 : -> key
    v         : -> value
    t         : -> table
  equations
    [1] look-up(k, empty-table) = default-value
    [2] look-up(k1, add(k2, v, t)) = if(eq(k1, k2), v, look-up(k1, t))
end tables

```

5.2. Data types specific to the transit node

The module *time* supplies functions to deal with timing information. To the outside the sort *time* is built up from the constant *initial-time*, using the *+*-function to add durations. A *duration* is either the constant *tick-duration*, or the difference of two times. Internally we use the *naturals* and auxiliary functions to define the exported functions.

```

data module time
begin
  exports
  begin
    sorts time, duration
    functions
      initial-time :                -> time
      tick-duration :              -> duration
      lt           : duration # duration -> BOOL
      _ + _       : time # duration  -> time
      _ - _       : time # time      -> duration
    end
  end

  imports natural-numbers

  functions
    time      : nat -> time
    duration  : nat -> duration

  variables
    n1, n2 : -> nat

  equations
    [1] initial-time           = time(0)
    [2] tick-duration         = duration(s(0))
    [3] lt(duration(n1), duration(n2)) = lt(n1, n2)
    [4] time(n1) + duration(n2)      = time(n1 + n2)
    [5] time(n1) - time(n2)          = duration(n1 - n2)

end time

```

The type of information that can be transmitted through the transit node is defined in the module *datum*.

```

data module datum
begin
  exports
  begin
    sorts datum
  end

  imports natural-numbers

  functions
    datum : nat -> datum

end datum

```


The transit nodes contains a number of ports for input and output. These ports are named with natural numbers. Port names can be collected into sets by binding the parameter of the basic module *set* to *port-name*.

```

data module port-name
begin

  exports
  begin
    sorts
      port-name
    functions
      eq : port-name # port-name -> BOOL
  end

  imports natural-numbers
  functions
    port-name : nat -> port-name

  variables
    n1, n2 : -> nat
  equations
    [1] eq(port-name(n1), port-name(n2)) = eq(n1, n2)

end port-name

data module port-sets
begin

  imports
  set
  { renamed by
    [ set      -> port-set,
      empty-set -> empty-port-set ]
    items bound by
    [ item      -> port-name ]
    to port-name
    equality bound by
    [ eq        -> eq ]
    to port-name
  }

end port-sets

```

A *route* consists of a *route-name* and a set of output ports associated with this route. Routes are collected into tables in order to look up the port-set corresponding to the name of a previously created route.

```

data module route-names
begin

  exports
  begin
    sorts
      route-name
    functions
      eq : route-name # route-name -> BOOL
  end

end

```

```

imports natural-numbers
functions
  route-name : nat -> route-name

variables
  n1, n2 : -> nat
equations
  [1] eq(route-name(n1), route-name(n2)) = eq(n1, n2)

end route-names

data module routes
begin

  exports
    begin
      sorts route
      functions
        route : route-name # port-set -> route
        name-of : route -> route-name
        ports-of : route -> port-set
        eq : route # route -> BOOL
      end
    end

  imports booleans, port-sets, route-names

  variables
    n1, n2 : -> route-name
    ps1, ps2 : -> port-set
  equations
    [1] name-of(route(n1, ps1)) = n1
    [2] ports-of(route(n1, ps1)) = ps1
    [3] eq(route(n1, ps1), route(n2, ps2)) = and(eq(n1, n2), eq(ps1, ps2))

end routes

data module route-tables
begin

  imports
    tables
    {renamed by
      [ table -> route-table,
        empty-table -> empty-route-table]
    items bound by
      [ key -> route-name,
        value -> port-set,
        eq -> eq,
        default-value -> empty-port-set]
    to routes}

end route-tables

```

If components communicate to the outside world or to each other, messages are exchanged. Most of the messages are indexed with a value of some data type. Messages can be collected in bags.

```

data module messages
begin
    exports
    begin
        sorts message
        functions
            add-datum-port : port-name      -> message
            add-route      : route          -> message
            send-faults    :                -> message
            routed-datum   : route-name # datum -> message
            req-route      : route-name      -> message
            available-ports : port-set       -> message
            timed-message   : time # datum   -> message
            datum           : datum          -> message
        end
    end

    imports datum, time, port-name, routes
end messages

data module message-bags
begin
    imports
    bags
    { renamed by
        [ bag      -> message-bag,
          empty-bag -> empty-message-bag ]
      items bound by
        [ item      -> message ]
        to messages
    }
end message-bags

```

The various components of the transit node are connected to each other with *channels*. There are also channels to the environment.

```

data module channels
begin
    exports
    begin
        sorts channel
        functions
            control-input      :                -> channel
            control-output     :                -> channel
            control-in-to-out  :                -> channel
            control-to-data    : port-name      -> channel
            data-to-control    : port-name      -> channel
            rejection          :                -> channel
            data-in-to-out     : port-name # port-name -> channel
            data-input         : port-name      -> channel
            data-output        : port-name      -> channel
        end
    end

    imports port-name
end channels

```

5.3. The processes

5.3.1. **Communication** The module *communication* defines the atomic actions that can be executed by the various components, when trying to communicate. The communication function is defined such that a read action (*r*) and a send action (*s*) can be combined into a communication action (*c*). These actions are indexed with the channel used to communicate and the message to be transmitted. In the same way timing information can be communicated.

The set of internal actions (*I*) and the set of actions to be encapsulated in order to get only successful communication (*H*) are also defined.

```

process module communication
begin

  exports
  begin
    atoms
      r                : channel # message
      s                : channel # message
      c                : channel # message
      read-time        : time
      send-time         : time
      comm-time         : time

    sets of atoms
      I = { c(c, m), comm-time(t) |
            t in time, c in internal-channels, m in message }
      H = { r(c, m), s(c, m), send-time(t), read-time(t) |
            t in time, c in internal-channels, m in message }

    end

  imports
    channels,
    messages,
    time

  sets of channel
    internal-channels =
    { control-in-to-out, rejection,
      data-to-control(pn1), control-to-data(pn1),
      data-in-to-out(pn1, pn2) | pn1 in port-name, pn2 in port-name }

  communications
    r(c, m) | s(c, m) = c(c, m)
    for c in channel, m in message
    read-time(t) | send-time(t) = comm-time(t)
    for t in time

end communication

```


5.3.2. *Data-ports-in* For every *port-name* a process *data-port-in* is defined. Every *data-port-in* behaves as follows. First it reads from its input channel the message to send some datum along some route. Then it reads the current time and asks the *control-port-in* for the port set attached to the requested route. Then a transit attempt is made. If the route-name was faulty, an empty-port-set was returned and the incoming message is routed to the rejection channel, thus becoming faulty. If the port-set was not empty, one port is selected randomly and after adding a time stamp the incoming message is routed to that port. The process *transit-datum* is not defined in case the port-set is empty. This means that it equals deadlock.

```

process module data-ports-in
begin

  exports
  begin
    processes
      data-port-in : port-name
    end
  end

  imports
    port-sets,
    route-names,
    time,
    communication

  processes
    transit-attempt : port-set # port-name # time # route-name # datum
    transit-datum   : port-set # port-name # time # datum

  variables
    t1, t2 : -> time
    p1, p2 : -> port-name
    rn      : -> route-name
    ps      : -> port-set
    d       : -> datum

  definitions
    data-port-in(p1) = sum(d in datum, sum(rn in route-name,
      r(data-input(p1), routed-datum(rn, d)) .
      sum(t1 in time, read-time(t1) . s(data-to-control(p1), req-route(rn)) .
      sum(ps in port-set, r(control-to-data(p1), available-ports(ps)) .
      transit-attempt(ps, p1, t1, rn, d) .
      data-port-in(p1))))))

    transit-attempt(empty-port-set, p1, t1, rn, d) =
      s(rejection, routed-datum(rn, d))
    transit-attempt(add(p2, ps), p1, t1, rn, d) =
      transit-datum(add(p2, ps), p1, t1, d)

    transit-datum(add(p2, ps), p1, t1, d) =
      s(data-in-to-out(p1, p2), timed-message(t1, d)) +
      transit-datum(ps, p1, t1, d)

end data-ports-in

```

5.3.3. Data-ports-out The following module is parameterized with a duration, max-transit-time, that determines the maximum time a message may stay within the transit node.

For every *port-name* a process *data-port-out* is defined. Every *data-port-out* is indexed with a bag of messages that must be sent to the environment. Initially this bag is empty. It starts by reading a timed message from one of the data-input-ports. This message is added to the bag and the process starts again. If the bag is not empty, the process also has the possibility to output some message from the bag. If the max-transit-time is expired, then the message becomes faulty and will be sent to the rejection channel. Otherwise, the message is sent to the environment.

```

process module data-ports-out
begin

  parameters
    max-transit-time
  begin
    functions
      max-transit-time : -> duration
    end max-transit-time

  exports
    begin
      processes
        data-port-out : port-name # message-bag
      end

  imports
    port-name,
    message-bags,
    communication

  processes
    handle-message-out : BOOL # datum # port-name

  variables
    t, t1, t2 : -> time
    p1, p2    : -> port-name
    mb        : -> message-bag
    d, e      : -> datum

  definitions
    data-port-out(p2, empty-message-bag) =
      sum(p1 in port-name, sum(t1 in time, sum(d in datum,
        r(data-in-to-out(p1, p2), timed-message(t1, d)) .
        data-port-out(p2, add(timed-message(t1, d), empty-message-bag))))))
    data-port-out(p2, add(timed-message(t2, e), mb)) =
      sum(p1 in port-name, sum(t1 in time, sum(d in datum,
        r(data-in-to-out(p1, p2), timed-message(t1, d)) .
        data-port-out(p2,
          add(timed-message(t1, d), add(timed-message(t2, e), mb)))))) +
      sum(t in time, read-time(t) .
        handle-message-out(lt(t - t2, max-transit-time), e, p2) .
        data-port-out(p2, mb))

    handle-message-out(false, d, p2) =
      s(rejection, datum(d))
    handle-message-out(true, d, p2) =
      s(data-output(p2), datum(d))

end data-ports-out

```

5.3.4. *Control-port-in* The process *control-port-in* keeps track of all defined routes and all existing ports, so it is indexed with a *route-table* and a *port-set*. It is connected to the environment with the *control-input* channel. Via this channel it can receive the message to add a datum-port, to add a route, or to flush all faulty messages. As a last option it can receive a request from some *data-port-in* to send the routing information belonging to some *route-name*. All these incoming messages are treated separately. The request to add a datum port is handled using a subprocess. This handler checks whether the data port already exists. Then it either rejects the message or adds the port to the *port-set* and creates two new parallel processes: a *data-port-in* and a *data-port-out*. If a request is made to add a route, it simply adds the route information to the *route-set*. A *send-faults* request is simply passed on to the *control-port-out*. A request for route information is answered by looking up the requested information and sending it back.

```

process module control-port-in
begin

  exports
  begin
    processes
      control-port-in : route-table # port-set
    end
  end

  imports
    route-tables,
    communication,
    data-ports-in,
    data-ports-out

  processes
    handle-add-port : route-table # port-set # port-name # BOOL

  variables
    p : -> port-name
    rt : -> route-table
    ps : -> port-set

  definitions
    control-port-in(rt, ps) =
      sum(p in port-name, r(control-input, add-datum-port(p)) .
        handle-add-port(rt, ps, p, element(p, ps)))
      + sum(r in route, r(control-input, add-route(r)) .
        control-port-in(add(name-of(r), ports-of(r), rt), ps))
      + r(control-input, send-faults) .
        s(control-in-to-out, send-faults) .
        control-port-in(rt, ps)
      + sum(p in port-name, sum(rn in route-name,
        r(data-to-control(p), req-route(rn)) .
        s(control-to-data(p), available-ports(look-up(rn, rt)))) .
        control-port-in(rt, ps)
    handle-add-port(rt, ps, p, true) =
      s(rejection, add-datum-port(p)) .
      control-port-in(rt, ps)
    handle-add-port(rt, ps, p, false) =
      control-port-in(rt, add(p, ps)) ||
        data-port-in(p) || data-port-out(p, empty-message-bag)

  end control-port-in

```

5.3.5. **Control-port-out** The process control-port-out is indexed with the *message-bag* containing all faulty messages. It has a simple behaviour. It can receive the message to send all faulty messages to the environment, which is handled by the subprocess *flush*, or it can receive faulty message via the rejection channel.

```

process module control-port-out
begin

  exports
  begin
    processes
      control-port-out : message-bag
    end
  end

  imports
    message-bags,
    communication

  processes
    flush : message-bag

  variables
    m : -> message
    mb : -> message-bag

  definitions
    control-port-out(mb) =
      r(control-in-to-out, send-faults) . flush(mb)
      + sum(m in message, r(rejection, m) .
        control-port-out(add(m, mb)))

    flush(empty-message-bag) = control-port-out(empty-message-bag)
    flush(add(m, mb)) = s(control-output, m) . flush(mb)

  end control-port-out

```

5.3.6. **Transit-node** Finally the transit node is specified by the concurrent operation of the *clock* process, which is a parameter of the system, the *control-port-in* and the *control-port-out*. These ports are initialized with an empty table, set and bag. In order to hide internal actions and to get only successful communication, we add the hiding operator and the encapsulation operator. Note that apart from the parameter *clock*, we also inherit the parameter *max-transit-time* from the imported module *data-ports-out*.

```

process module transit-node
begin

  parameters
    time
  begin
    processes
      clock
    end time

```



```

exports
  begin
    processes
      transit-node
    end

imports
  control-port-in,
  control-port-out

definitions
  transit-node = hide(I, encaps(H,
    clock ||
    control-port-in(empty-route-table, empty-port-set) ||
    control-port-out(empty-message-bag)))

end transit-node

```

5.4. Example of a clock

In this section we give an example of how the clock parameter of the transit node can be initialized. The process *clock* starts at the *initial-time*. Then it can do a *tick*, followed by an increment of the current time with a *tick-duration*, or it can send the time to anyone willing to read it. Note that in this version of a clock the action of sending the time will not cost any time.

```

process module a-clock
begin

  exports
    begin
      processes
        clock
      end

  imports
    time,
    communication

  atoms
    tick

  processes
    clock : time

  variables
    t : -> time

  definitions
    clock = clock(initial-time)
    clock(t) = tick . clock(t + tick-duration) +
      send-time(t) . clock(t)

end a-clock

```

```

process module transit-node-with-a-clock
begin

  imports
    transit-node
    {time bound by
      [clock -> clock]
    to a-clock}

end transit-node-with-a-clock

```

5.5. Graphical representation of the import relation

Using the IDEAS tool developed within the METEOR project [Ide88] we can give the following picture (see figure 2), representing the import relation between all modules of the specification of the transit node. Rectangular boxes are used for data modules and boxes with rounded corners are used for process modules. An arrow from a module to another module means that the former is imported into the latter. Note that not all textual imports are present in the picture. We used a tool to compute the minimal import relation having the same transitive closure as the textual one.

6. RELATION TO THE ERAE SPECIFICATION

In this section we will give a brief discussion of the relation between the ERAE specification and the PSF_d specification of the transit node. It is clear that, since ERAE was designed for requirements specification, the first one is closer to the textual specification, whereas in the second one some design decisions had to be made. As an example look at the routing information that is treated as a separate entity in ERAE, while in PSF_d it is part of the state of the *control-port-in*.

The ERAE language is based on temporal logic. Its formal semantics can be found in [HR89], and [DHR88] contains an introduction to the use of ERAE.

In order to validate that a PSF_d specification is correct with respect to an ERAE specification, a formal treatment of this notion of validation would be needed. Since this paper does not focus on this subject, we only give some informal reasoning about the relation between the two specifications.

The validation is made up of two parts. First we must give a relation between the entities declared in the ERAE specification and the ones declared in the PSF_d specification, and then we must provide an interpretation of the temporal statements in ERAE into PSF_d .

6.1. Entities

A quick inspection learns that, apart from some design decisions and detail implementations, the entities in ERAE relate to the entities in PSF_d having the same name. So where ERAE contains messages like *Add-route msgs* indexed with a *route nr* and a series of *out port-nr*, PSF_d has a data type *messages*, containing a function *add-route*, indexed with *route* which is a combination of a *route-name* and a *port-set*.

As an other example look at the entity *Data port-in* which is indexed with a *nr*, and is able to receive *Data msgs* via a *port*. In PSF_d this translates to a process *data-port-in*, indexed with a *port-name*, having a channel to the environment called *data-input*, via which it can receive a *routed-datum*.

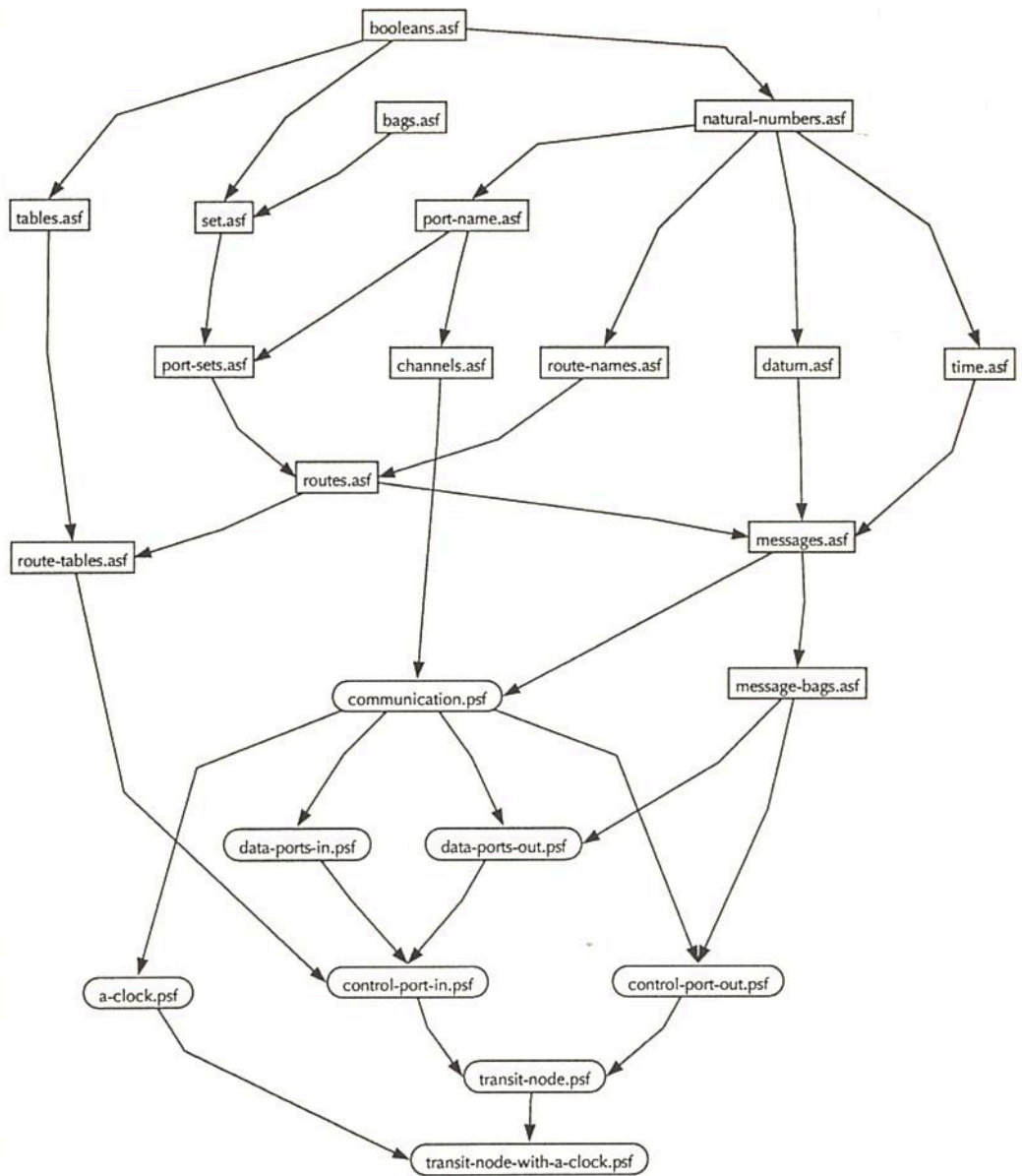


figure 2 The import relation

6.2. Temporal statements

Naively speaking the interpretation of a temporal statement in ERAE into PSF_d consists of an interpretation of all events involved into atomic actions, followed by a verification that every possible trace of the specification in PSF_d satisfies all temporal statements about events given in the ERAE specification. Unfortunately this approach is too simple since not only temporal information is involved but also information about the state space of the system.

As an example of how to informally validate the PSF_d specification, we will give some ERAE statements and their informal interpretation in the PSF_d specification.

$$\begin{aligned} \text{initially} \Rightarrow & \neg \exists \text{ dpi: is-in}(\text{dpi}, \text{Data-ports-in}) \\ & \wedge \neg \exists \text{ dpo: is-in}(\text{dpo}, \text{Data-ports-out}) \\ & \wedge \neg \exists r: \text{is-in}(r, \text{Routes}) \\ & \wedge \neg \exists \text{ wm, dm: faulty}(\text{wm}) \vee \text{faulty}(\text{dm}) \end{aligned}$$

This can be interpreted as the statement that there are no data ports in the definition of the process *transit-node*, and that the *port-set*, *route-table* and (faulty) *message-bag* are empty:

```
transit-node = hide(I, encaps(H,
  clock ||
  control-port-in(empty-route-table, empty-port-set) ||
  control-port-out(empty-message-bag)))
```

A number of statements are about the behaviour of the environment of the transit node. These statements are not explicitly met by the PSF_d specification, since it only specifies the behaviour of the transit node without restricting its environment. As an example look at the statement

$$\text{occurs}(\text{dm}) \Rightarrow \bullet \text{ exists}(\text{port}(\text{dm}))$$

which states that messages only arrive at existing input ports (the symbol \bullet means "true in the previous state"). This assumption about the environment is not stated in the PSF_d specification.

As a last example look at the statement about state changes concerning *data-ports-in*:

$$\begin{aligned} & \text{exists}(\text{dpi}) \wedge \bullet \neg \text{exists}(\text{dpi}) \\ & \Rightarrow \exists \text{ apm: occurs}(\text{apm}) \wedge \text{nr}(\text{dpi}) = \text{port-nr}(\text{apm}) \end{aligned}$$

This states that if a *data-port-in* is created, an add-port-message must have been occurred. In the PSF_d specification this is verified by looking at all places where a *data-port-in* is created. This can only happen in the subprocess *handle-add-port* of the process *control-port-in*. This subprocess is only invoked after the atomic action $c(\text{control-input}, \text{add-datum-port}(p))$ has occurred for some appropriate *port-name* p .

It is clear that this reasoning is very informal. This is because the existence of a *data-port-in* is easy to check at the textual level of the specification, but not at the level of the semantics of PSF_d . The semantics is a labeled transition graph, which in no way contains information about the number of processes that it is constructed from, but only about the actions that can be performed by the system. Also the actual value of the indexes of the processes involved is not part of the semantics.

7. DISCUSSION

Since some design decisions were needed, the specification of the transit node in PSF_d is more specific than the specification in ERAE. There is no easy transformation from an ERAE specification to a PSF_d specification, however when having an ERAE specification, the informal text can be interpreted more easily.

We can only give an informal validation of the PSF_d specification when relating it to the ERAE specification. This is due to the fact that in some cases ERAE statements relate to the state of the system, which is not part of the formal semantics of PSF_d . We can however look at the textual level of the specification and give an informal reasoning. Also restrictions to the environment can not be expressed in PSF_d .

The design of the specification can be generalized to the following method:

- Identify the parameters of the system.
- Identify all concurrent components.
- Add indexes to the process names of each component to keep track of state information and to create more instances of the object.
- Define the abstract data types needed for these indexes.
- Specify how the components are connected.
- Define the initial state of the system.
- Define the behaviour of each component.

Of course the last step of this method can be very involved. Each component in turn can then be divided into subcomponents, in such a way that the method recursively applies to these subcomponents.

As a conclusion we can state that PSF_d is well suited for the specification of concurrent systems.

8. ACKNOWLEDGEMENTS

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